



Effective  
Field  
Theory  
Gauge  
Lattice

## Symposium on Effective Field Theories and Lattice Gauge Theory

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# Hadronic matrix elements for Neutrino Cross sections

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VNIVERSITAT  
ID VALÈNCIA



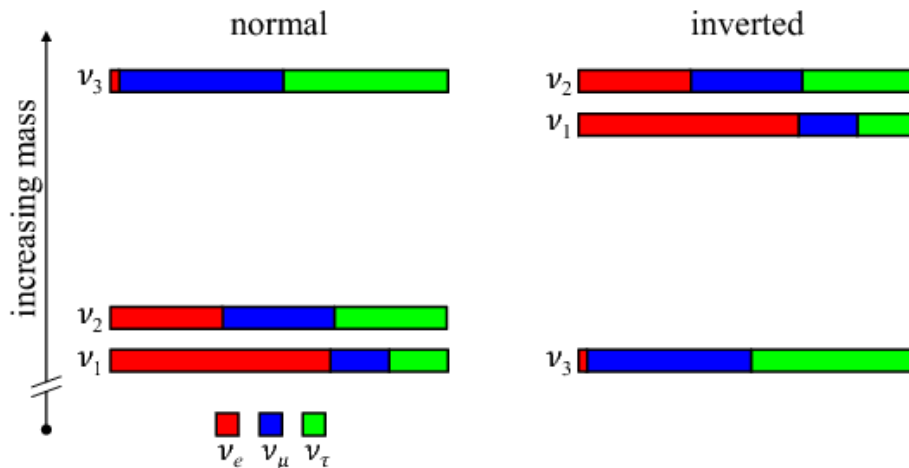
EXCELENCIA  
SEVERO  
OCHOA

# Introduction

- Neutrino interactions with matter are at the heart all experiments seeking to unravel its nature.
- Oscillation experiments (with accelerator  $\nu$  in the few-GeV region):  
T2K, NOvA, MicroBooNE, Hyper-K, DUNE/LBNF
  - Goals:  $\nu$  mass hierarchy, CP violation
  - Good understanding of neutrino interactions are important for:
    - $\nu$  detection, flavor ID
    - reduction of systematic errors
      - $E_\nu$  reconstruction,  $\nu$  flux calibration
      - determination of (irreducible) backgrounds
  - Precision of 1-5% in  $\nu$  cross sections might be required

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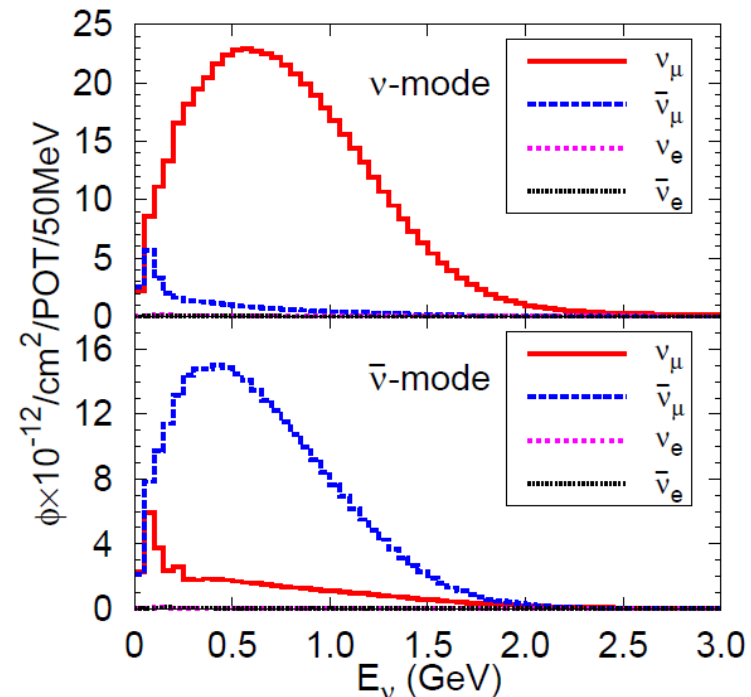
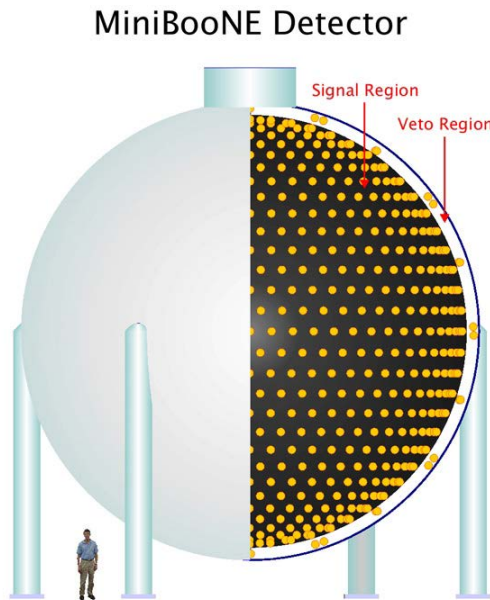
# $\nu$ experiments



# need you!

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  - E.g. in the **MiniBooNE**  $\nu_\mu \rightarrow \nu_e$  search



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- **Charged current quasielastic scattering** (CCQE)  $\nu_l n \rightarrow l^- p$

- $\bar{\nu}_l p \rightarrow l^+ n$

- $\nu$  detection and **flavor ID**

- Kinematic  $E_\nu$  reconstruction

$$E_\nu = \frac{2m_n E_\mu - m_\mu^2 - m_n^2 + m_p^2}{2(m_n - E_\mu + p_\mu \cos \theta_\mu)}$$

- Needed for **oscillation** studies:

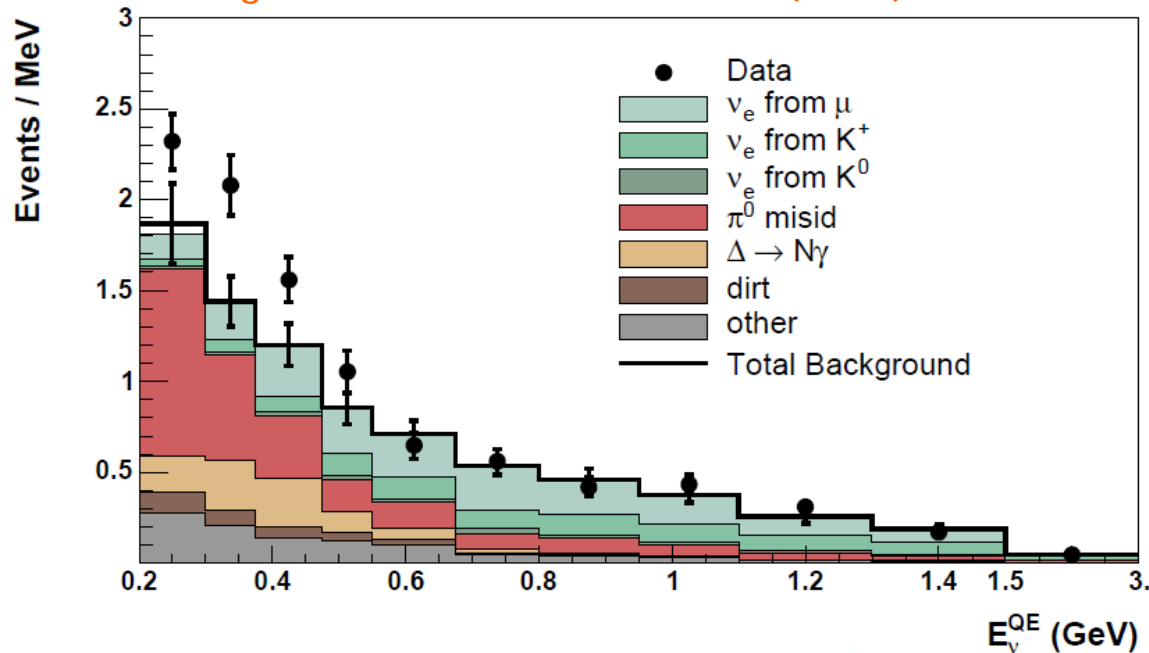
$$P(\nu_\mu \rightarrow \nu_\tau) = \sin^2 2\theta_{23} \sin^2 \frac{\Delta m_{23}^2 L}{4E_\nu}$$

# Relevance for oscillation experiments

- E.g. in the MiniBooNE  $\nu_\mu \rightarrow \nu_e$  search

- Backgrounds

Aguilar-Arevalo et al., PRL102 (2009) 101802



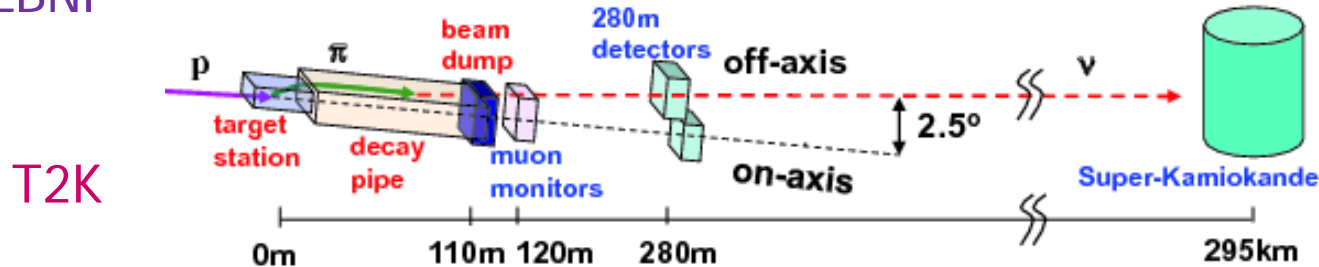
- NC backgrounds:  $\nu_l N \rightarrow \nu_l \pi^0 N'$   
 $\nu_l N \rightarrow \nu_l \gamma N'$

- Dominated by baryon resonance excitation



# Introduction

- Oscillation experiments (with accelerator  $\nu$  in the few-GeV region)
- Experiments with near & far detectors: T2K, NOvA, MicroBooNE, Hyper-K, DUNE/LBNF



- Near detectors help to reduce systematic errors:

$$\frac{N_{events}^{far}(E_\nu)}{N_{events}(E_\nu)} = \frac{\int \sigma(E'_\nu) \Phi(E'_\nu) P(E_\nu | E'_\nu) P_{osc}(E'_\nu) dE'_\nu}{\int \sigma(E'_\nu) \Phi(E'_\nu) P(E_\nu | E'_\nu) dE'_\nu}$$

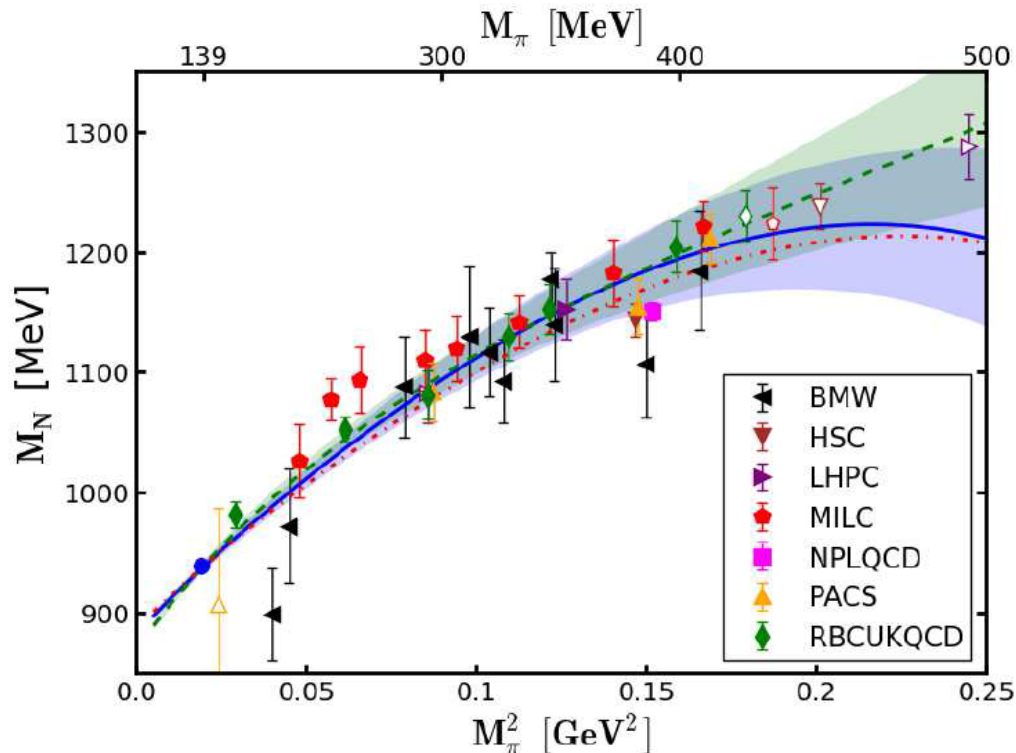
F. Sanchez @ NuPhys2015

but c.s. uncertainties **do not cancel** (exactly) in the ratio

- exposed to different fluxes with different flavor composition
- different geometry, acceptance and targets

# Analogies with direct DM searches

- XENON, LUX, ...
- Spin independent **WIMP-Nucleus** cross section  $\sim \sigma_{\pi N}^2$
- $\pi N$  sigma term can be extracted using **ChPT** + **IQCD**
- With SU(2)  $p^4$  **covariant BChPT** with  $\Delta(1232)$  LAR et al., PRD 88 (2013)



$N_f = 2 + 1$   
**Without**  $\Delta(1232)$ :  $\sigma_{\pi N} = 55(3)$  MeV  
**With**  $\Delta(1232)$ :  $\sigma_{\pi N} = 44(3)$  MeV

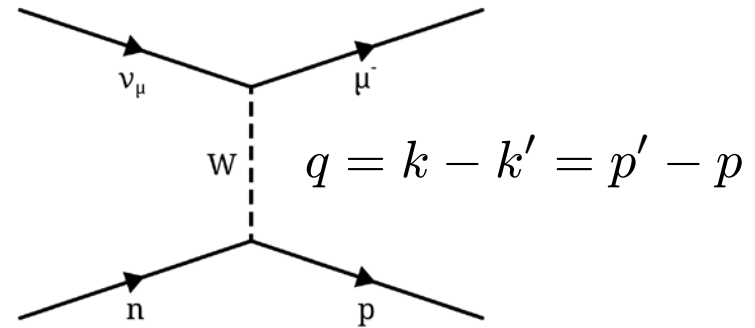
# QE scattering on the nucleon

CCQE :  $\nu(k) + n(p) \rightarrow l^-(k') + p(p')$

$\bar{\nu}(k) + p(p) \rightarrow l^+(k') + n(p')$

NCE :  $\nu(k) + N(p) \rightarrow \nu(k') + N(p')$

$\bar{\nu}(k) + N(p) \rightarrow \bar{\nu}(k') + N(p')$



$$\mathcal{M} = \frac{G_F \cos \theta_C}{\sqrt{2}} l^\alpha J_\alpha$$

where  $l^\alpha = \bar{u}(k') \gamma^\alpha (1 - \gamma_5) u(k)$

$$J_\alpha = \bar{u}(p') \left[ \gamma_\alpha F_1^V + \frac{i}{2M} \sigma_{\alpha\beta} q^\beta F_2^V + \gamma_\mu \gamma_5 F_A + \frac{q_\mu}{M} \gamma_5 F_P \right] u(p)$$

■ Vector form factors:  $F_{12}^V = F_{12}^p - F_{12}^n$

$$G_E = F_1 + \frac{q^2}{2m_N} F_2 \quad \leftarrow \text{electric}$$

$$G_M = F_1 + F_2 \quad \leftarrow \text{magnetic}$$

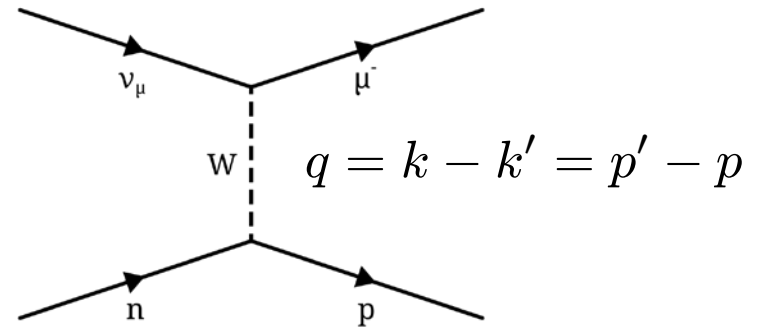
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■ Axial form factors:

$$F_A(Q^2) = g_A F(Q^2), \quad F_P(Q^2) = \frac{2M^2}{Q^2 + m_\pi^2} F_A(Q^2), \quad Q^2 = -q^2 > 0$$

$g_A = 1.267 \leftarrow \beta \text{ decay}$

PCAC

# QE scattering on the nucleon

- Axial form factor:  $Q^2$  dependence

- CCQE on H and D (BNL, ANL) ← early 80s

$$F_A(Q^2) = g_A \left(1 + \frac{Q^2}{M_A^2}\right)^{-2} \quad \langle r_A^2 \rangle = \frac{12}{M_A^2}$$

- $M_A = 1.016 \pm 0.026$  GeV Bodek et al., EPJC 53 (2008)

- From  $\pi$  electroproduction on p: Bernard et al., PRL69 (1992)

$$6 \left. \frac{dE_{0+}^{(-)}}{dq^2} \right|_{q^2=0} = \langle r_A^2 \rangle + \frac{3}{M} \left( \kappa^V + \frac{1}{2} \right) + \frac{3}{64f_\pi^2} \left( 1 - \frac{12}{\pi^2} \right)$$

- $M_A = 1.014 \pm 0.016$  GeV Liesenfeld et al., PLB 468 (1999) 20

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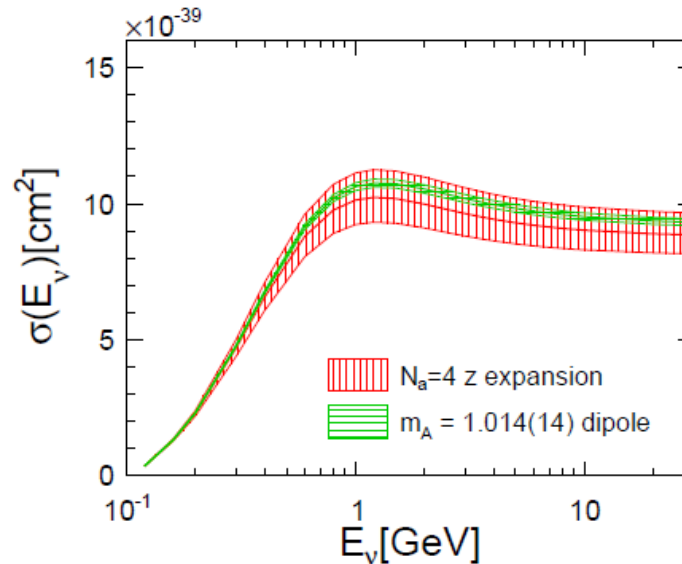
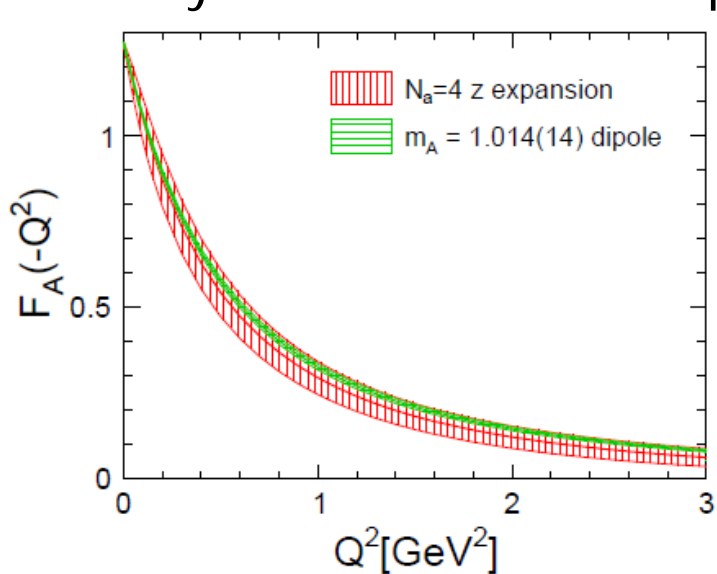
## ■ Dipole ansatz

- Not theoretically justified
- Leads to artificially small errors in  $M_A$

$$F_A(Q^2) = g_A \left(1 + \frac{Q^2}{M_A^2}\right)^{-2}$$

## ■ z-expansion Meyer et al., arXiv:1603.03048

- Fit to ANL, BNL, FNAL data
- Systematic errors: acceptance and deuteron corrections

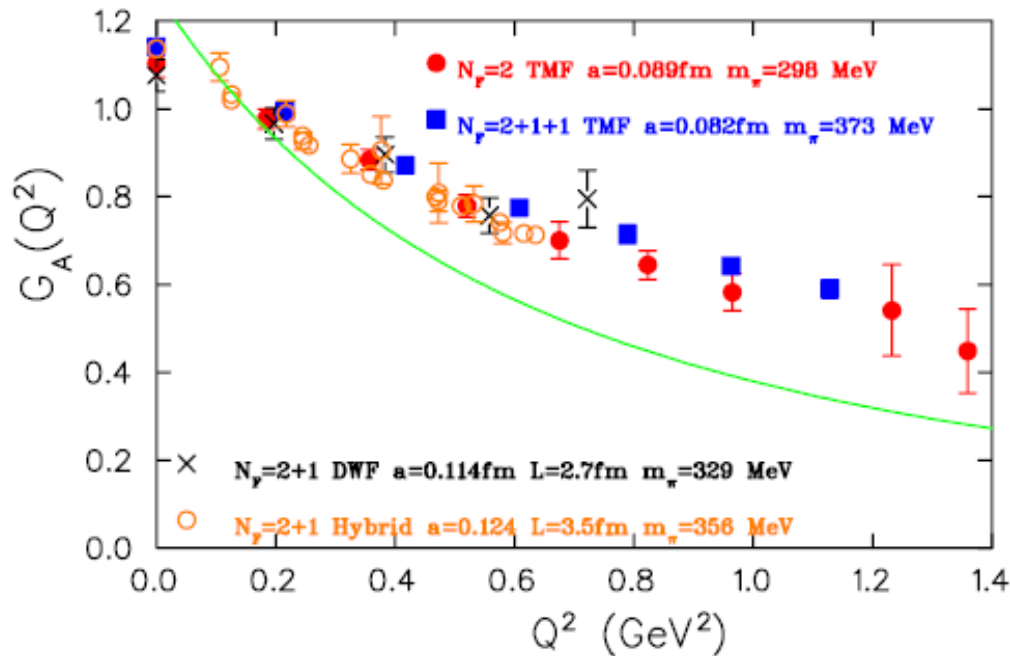


- $\langle r_A^2 \rangle = 0.46(22) \text{ fm}^2$  vs  $0.453(12) \text{ fm}^2$  Bodek et al., EPJC 53 (2008)



# $F_A$ & IQCD

- More precise information about  $F_A$ 
  - New CCQE measurements on D/H target
  - IQCD



Alexandrou et al., PRD 88 (2013)

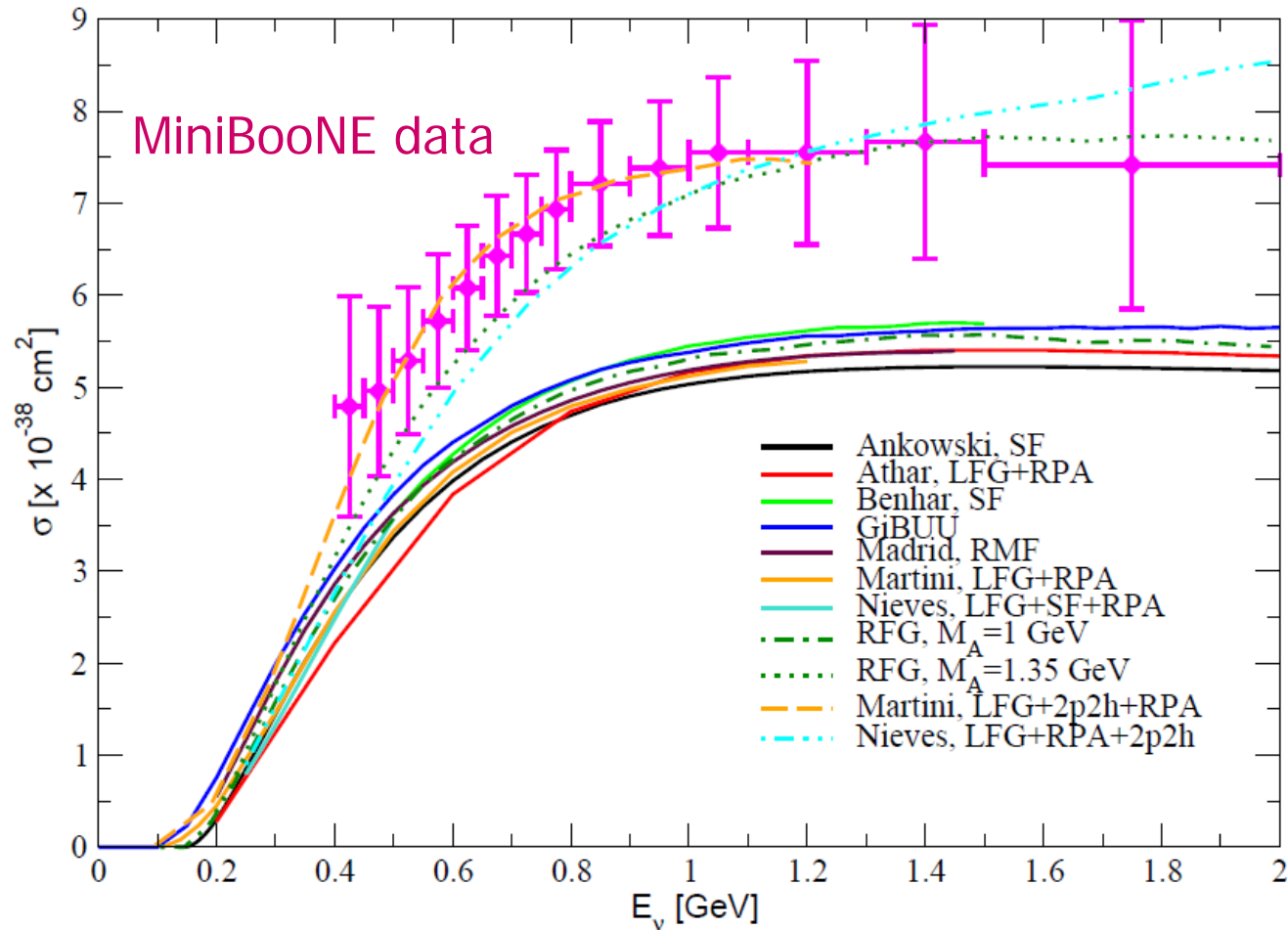
■  $m_\pi = 373$  MeV  $\Rightarrow M_A = 1.60(5)$  GeV  $\Leftrightarrow \langle r_A^2 \rangle = 0.183(6)$  fm<sup>2</sup>

■ Modern data?

# CCQE on nuclear targets

The problem:

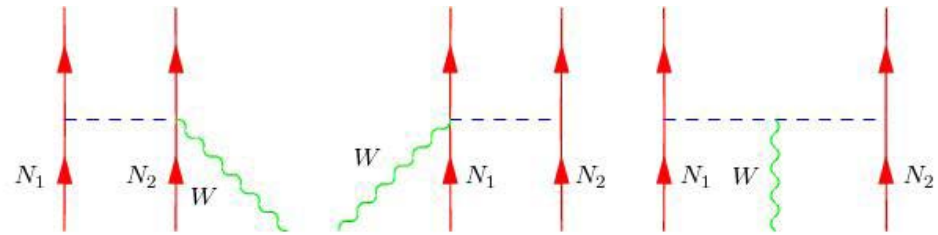
CCQE on  $^{12}\text{C}$



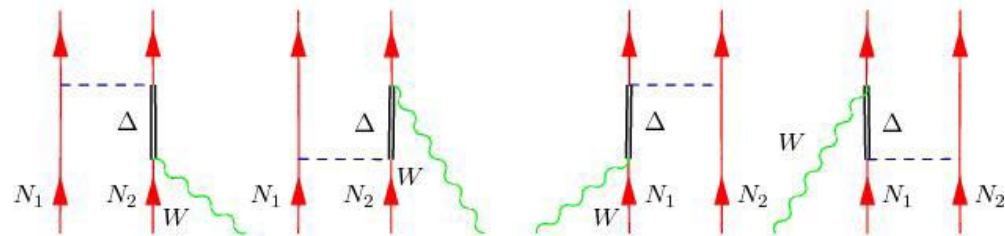
# CCQE-like on nuclear targets

The solution:

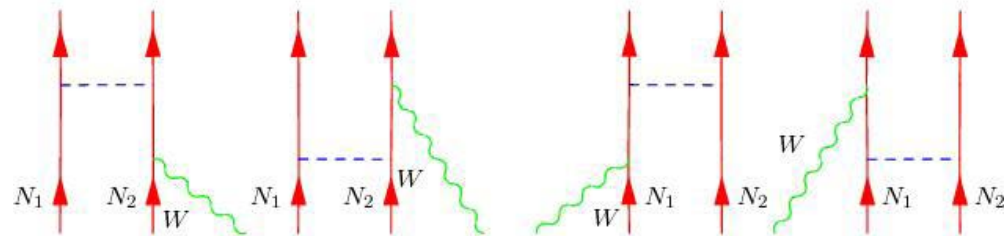
- multinucleon (2p2h) contributions
  - Martini et al., PRC 80 (2009)
  - Nieves et al., PRC 83 (2011)
  - Amaro et al., PLB 696 (2011)
- + RPA (important at low  $Q^2$ )



Contact and *pion-in-flight* diagrams



$\Delta$ -Meson Exchange Current diagrams



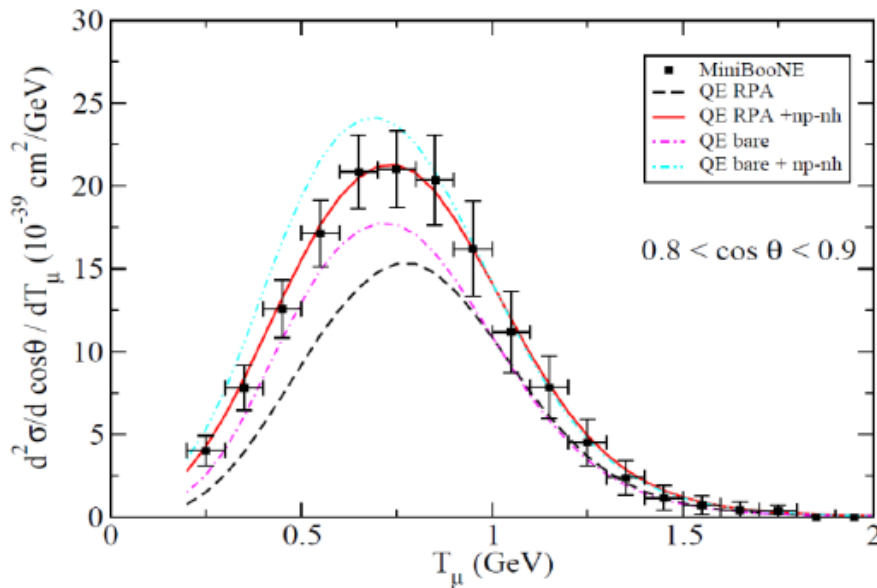
Correlation diagrams

# CCQE-like on nuclear targets

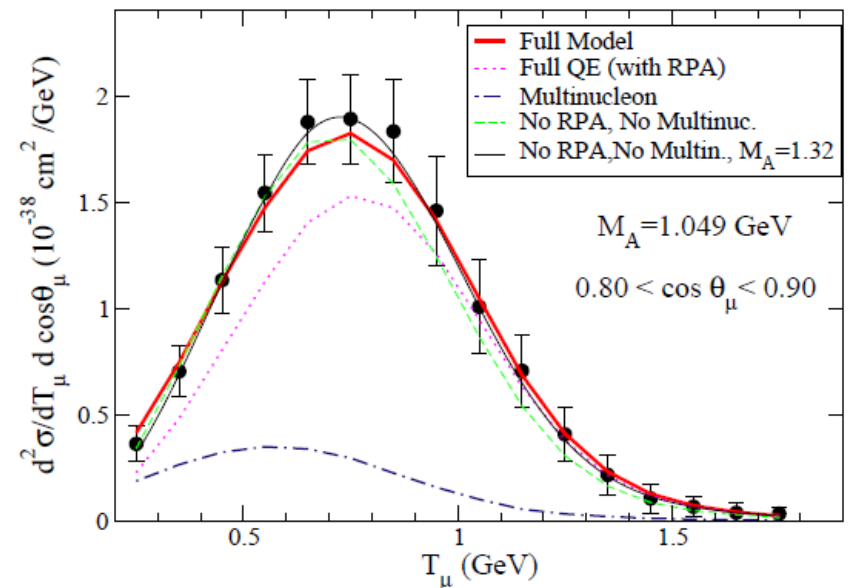
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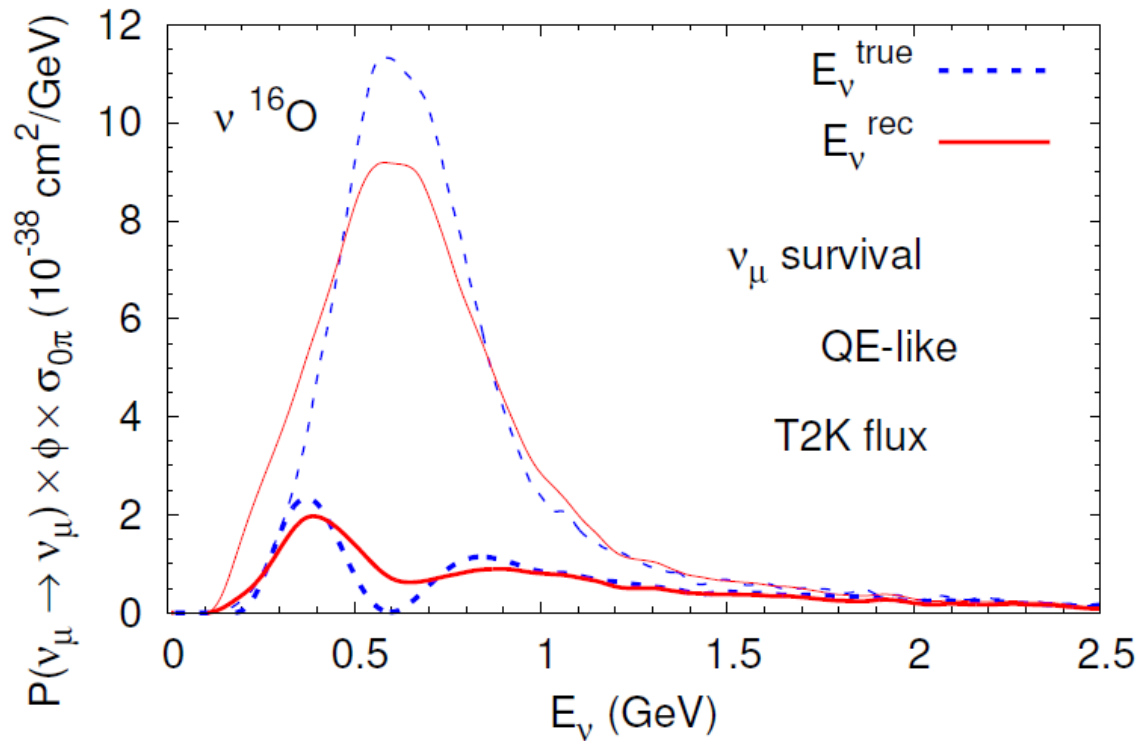
Martini et al.



Nieves et al.



# 2p2h and $E_\nu$ energy reconstruction



- $E_\nu$  misreconstruction is bound to have an impact **oscillation analyses**  
Lalakulich, Mosel, PRC 86 (2012); Coloma, Huber, PRL 111(2013); Jen et al., PRD 90 (2014)
- Bias remains after the **ND** is taken into account

# *Ab initio* Quantum MC method

- Solution of the **quantum many-body problem** for **nuclear** Hamiltonians
  - **NN & NNN** forces
- Computation of Euclidean (Im time) responses  
= Laplace transforms of **Response functions**

$$\left( \frac{d\sigma}{d\epsilon' d\Omega} \right)_{\nu/\bar{\nu}} = \frac{G_F^2}{2\pi^2} k' \epsilon' \cos^2 \frac{\theta}{2} \left[ R_{00} + \frac{\omega^2}{q^2} R_{zz} - \frac{\omega}{q} R_{0z} \right. \\ \left. + \left( \tan^2 \frac{\theta}{2} + \frac{Q^2}{2q^2} \right) R_{xx} \mp \tan \frac{\theta}{2} \sqrt{\tan^2 \frac{\theta}{2} + \frac{Q^2}{q^2}} R_{xy} \right],$$

- **1-body + 2-body** (nonrelativistic) currents
  - Cannot describe  $\pi$  production [static  $\Delta(1232)$  ]
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- Considerable computational effort:  $A \leq 12$
- **Significant** ( $\sim 30\%$ ) contribution from **2-body** current to the **transverse/interference** NC responses on  $^{12}\text{C}$   
A. Lovato et al., PRL 112 (2014); PRC 91 (2015)

# 2-nucleon currents in EFT and IQCD

- In **Chiral EFT** e.g. Barone et al., PRC93 (2016)
  - two-nucleon axial currents: OPE, TPE, CT
  - LO,..., N3LO
  - non-relativistic, no  $\Delta(1232)$  intermediate states
- In **IQCD**:
  - Two-body EM contributions to  $n p \rightarrow d \gamma$   
Beane et al., PRL 115 (2015)
  - **First step** toward the determination of EW two-nucleon interactions



# $1\pi$ production on the nucleon

$$\nu_l N \rightarrow l \pi N'$$

- CC:  $\nu_\mu p \rightarrow \mu^- p \pi^+$ ,  $\bar{\nu}_\mu p \rightarrow \mu^+ p \pi^-$   
 $\nu_\mu n \rightarrow \mu^- p \pi^0$ ,  $\bar{\nu}_\mu p \rightarrow \mu^+ n \pi^0$   
 $\nu_\mu n \rightarrow \mu^- n \pi^+$ ,  $\bar{\nu}_\mu n \rightarrow \mu^+ n \pi^-$

- source of CCQE-like events (in nuclei)

- needs to be subtracted for a good  $E_\nu$  reconstruction

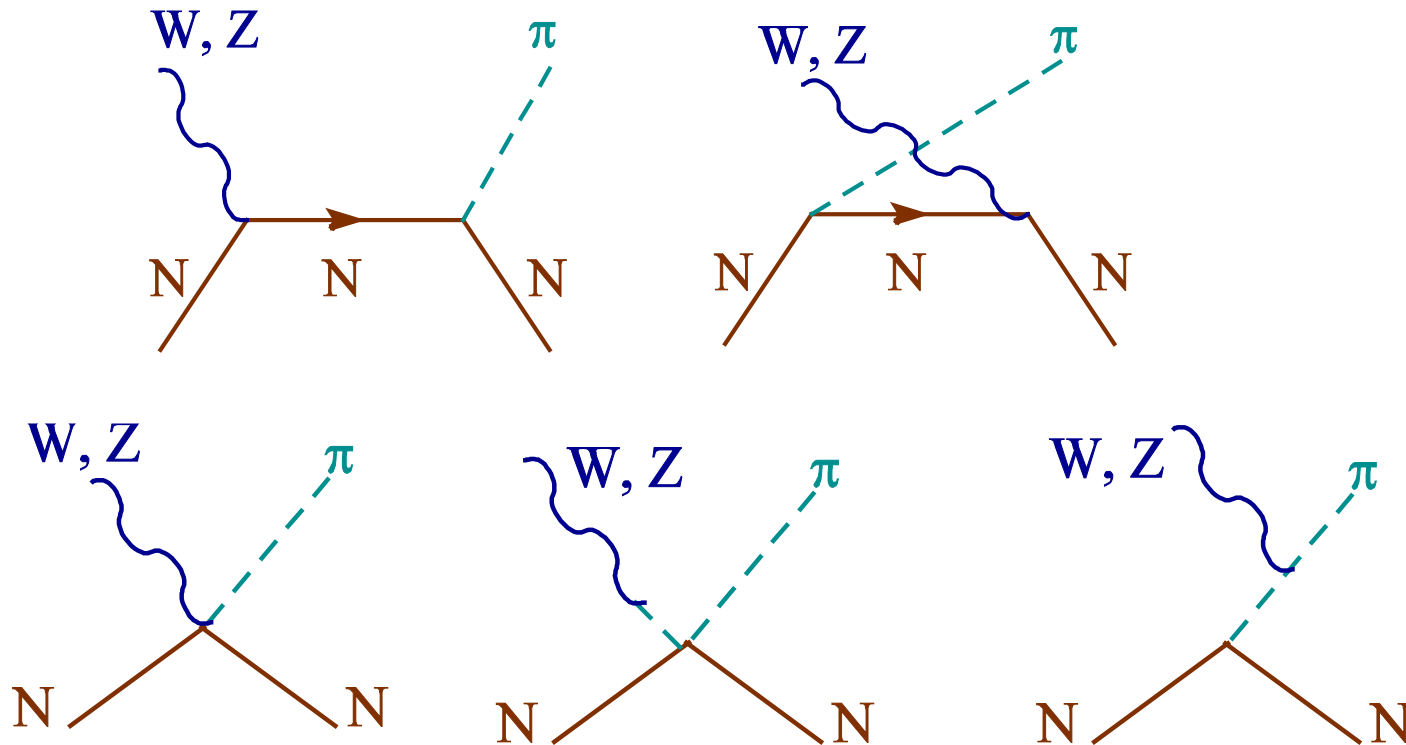
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 $\nu_\mu p \rightarrow \nu_\mu n \pi^+$ ,  $\bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu n \pi^0$   
 $\nu_\mu n \rightarrow \nu_\mu n \pi^0$ ,  $\bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu n \pi^0$   
 $\nu_\mu n \rightarrow \nu_\mu p \pi^-$ ,  $\bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu p \pi^-$

- e-like background to  $\nu_\mu \rightarrow \nu_e$  (T2K)

# $1\pi$ production on the nucleon

$$\nu_l N \rightarrow l \pi N'$$

- From **Chiral symmetry**:

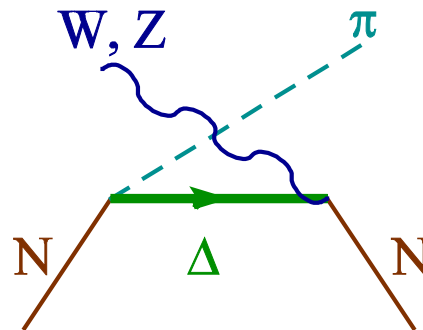
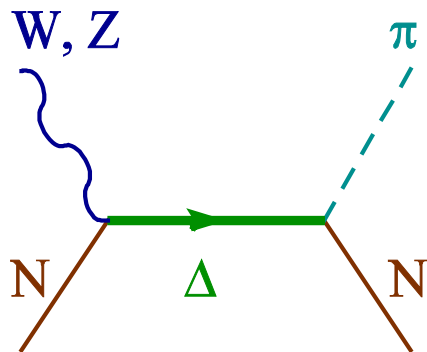


Hernandez et al., Phys.Rev. D76 (2007) 033005

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- $\Delta(1232)$  excitation:



# 1 $\pi$ production on the nucleon

- $\Delta(1232)$   $J^P=3/2^+$

$$J_\alpha = \bar{u}^\mu(p') \left[ \left( \frac{C_3^V}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^V}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\alpha p'_\mu) + \frac{C_5^V}{M_N^2} (g_{\alpha\mu} q \cdot p - q_\alpha p_\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^A}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\beta p'_\mu) + C_5^A g_{\alpha\mu} + \frac{C_6^A}{M_N^2} q_\alpha q_\mu \right] u(p)$$

$C_{3-5}^V, C_{3-6}^A \leftarrow$  N- $\Delta$  transition form factors

- Rarita-Schwinger fields: spin 3/2

$$u_\mu(p, s_\Delta) = \sum_{\lambda, s} \left( 1\lambda \frac{1}{2}s \middle| \frac{3}{2}s_\Delta \right) \epsilon_\mu(p, \lambda) u(p, s)$$

- Eq. of motion:  $(\not{p} - M_\Delta) u_\mu = 0$
- with constrains:  $\gamma^\mu u_\mu = p^\mu u_\mu = 0$

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- **Helicity amplitudes** are extracted from data on  $\pi$  photo- and electro-production in (model dependent) partial-wave analyses

$$A_{1/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 1/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = -1/2 \rangle \zeta$$

$$A_{3/2} = \sqrt{\frac{2\pi\alpha}{k_R}} \langle R, J_z = 3/2 | \epsilon_\mu^+ J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$

$$S_{1/2} = -\sqrt{\frac{2\pi\alpha}{k_R}} \frac{|\mathbf{q}|}{\sqrt{Q^2}} \langle R, J_z = 1/2 | \epsilon_\mu^0 J_{\text{EM}}^\mu | N, J_z = 1/2 \rangle \zeta$$

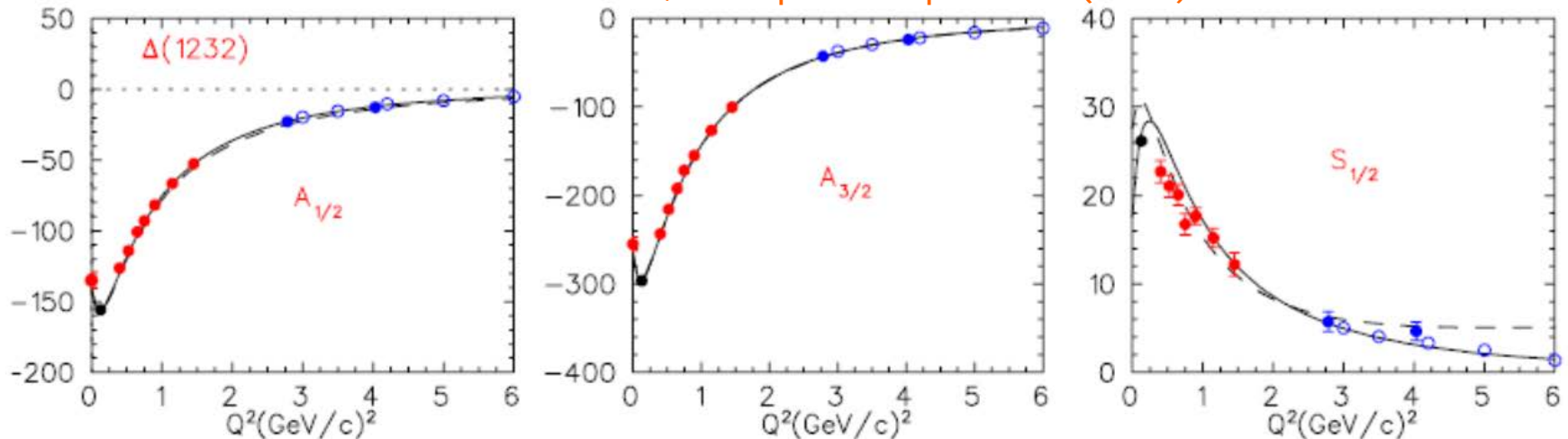
# Weak Resonance excitation

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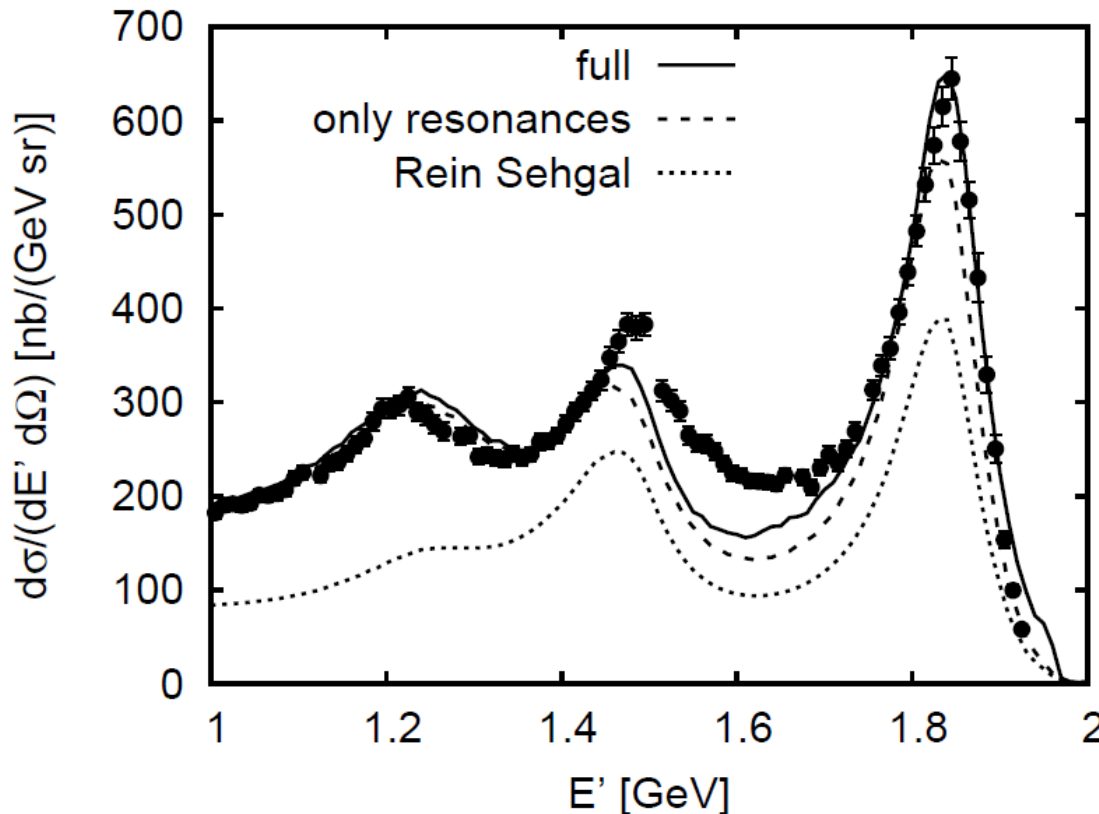
Tiator et al., EPJ Special Topics 198 (2011)



# $1\pi$ production on the nucleon

- Resonance excitation in  $\nu$  MC generators:
- Rein-Sehgal model: Rein-Sehgal, *Ann. Phys.* 133 (1981) 79.
- Helicity amplitudes for 18 baryon resonances; relativistic quark model
- **Poor description** of  $\pi$  electroproduction data on p

$e^- p \rightarrow e^- X, \theta = 20^\circ, E = 2.445 \text{ GeV}$



Leitner et al., POS NUFACT08

# Weak Resonance excitation

- $\Delta(1232)$   $J^P=3/2^+$

$$J_\alpha = \bar{u}^\mu(p') \left[ \left( \frac{C_3^V}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^V}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\alpha p'_\mu) + \frac{C_5^V}{M_N^2} (g_{\alpha\mu} q \cdot p - q_\alpha p_\mu) \right) \gamma_5 \right. \\ \left. + \frac{C_3^A}{M_N} (g_{\alpha\mu} \not{q} - q_\alpha \gamma_\mu) + \frac{C_4^A}{M_N^2} (g_{\alpha\mu} q \cdot p' - q_\beta p'_\mu) + C_5^A g_{\alpha\mu} + \frac{C_6^A}{M_N^2} q_\alpha q_\mu \right] u(p)$$

- Axial form factors

$$C_5^A(0) = \sqrt{\frac{2}{3}} g_{\Delta N \pi} \quad \leftarrow \text{off diagonal Goldberger-Treiman relation}$$

$$\mathcal{L}_{\Delta N \pi} = -\frac{g_{\Delta N \pi}}{f_\pi} \bar{\Delta}_\mu (\partial^\mu \vec{\pi}) \vec{T}^\dagger N \quad g_{\Delta N \pi} \Leftrightarrow \Gamma(N^* \rightarrow N \pi)$$

- Deviations from GTR arise from chiral symmetry breaking
- expected only at the few % level

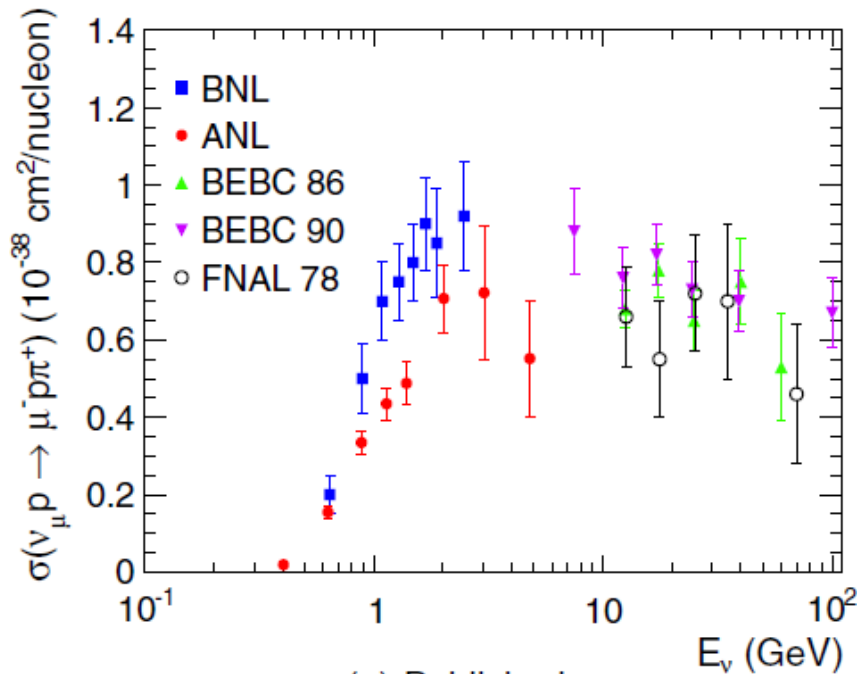


# $1\pi$ production on the nucleon

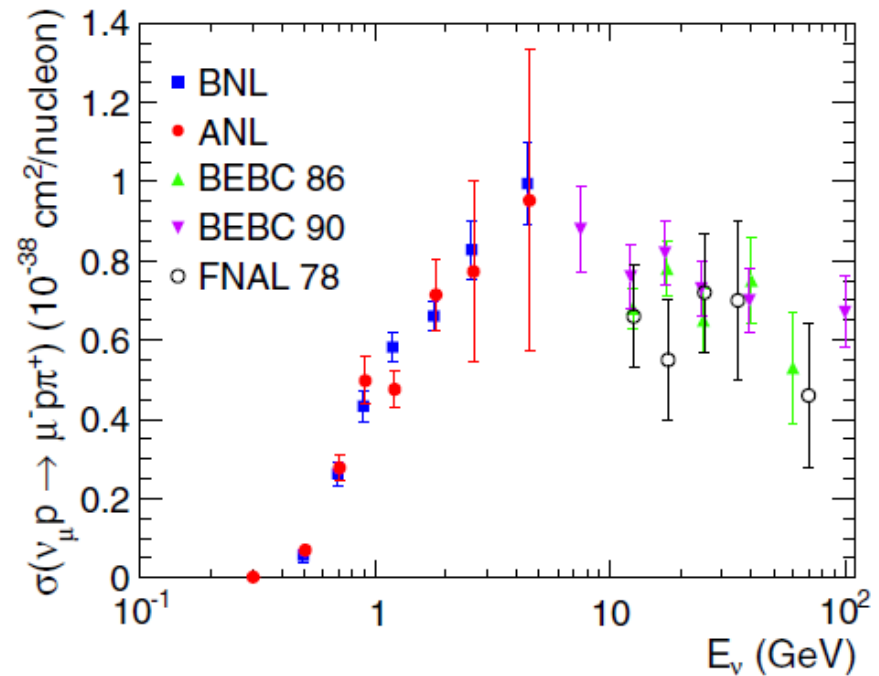
- **N- $\Delta$**  axial form factors: determination of  $C_5^A(0)$  and  $M_{A\Delta}$
- $C_5^A = C_5^A(0) \left(1 + \frac{Q^2}{M_{A\Delta}^2}\right)^{-2}$
- From **ANL** and **BNL** data on  $\nu_\mu d \rightarrow \mu^- \pi^+ p n$
- Hernandez et al., PRD 81 (2010)
  - Deuteron effects
  - $C_5^A(0) = 1.00 \pm 0.11$ ,  $M_{A\Delta} = 0.93 \pm 0.07$  GeV
  - **20% reduction** vs the **GT** relation  $C_5^A(0) = 1.15 - 1.2$
- LAR, Hernandez, Nieves, Vicente Vacas, PRD 93 (2016)
  - **Unitarization** in the leading vector and axial multipoles
  - Phases enforced to correspond to  $\pi N \rightarrow \pi N$  (**Watson's theorem**)
  - $C_5^A(0) = 1.12 \pm 0.11$ ,  $M_{A\Delta} = 0.95 \pm 0.06$  GeV
  - **Consistent** with the off-diagonal **GT** relation  $C_5^A(0) = 1.15 - 1.2$

# $1\pi$ production on nucleons

- **Discrepancies** between **ANL** and **BNL** datasets



(a) Published



(b) This analysis

- **Reanalysis** by **Wilkinson et al., PRD90 (2014)**

- **Flux normalization independent ratios:**  $CC1\pi^{+} / CCQE$

- **Good agreement** for ratios

- Better understood  $CCQE$  cross section used to obtain the  $CC1\pi^{+}$  one

# $1\pi$ production on nucleons

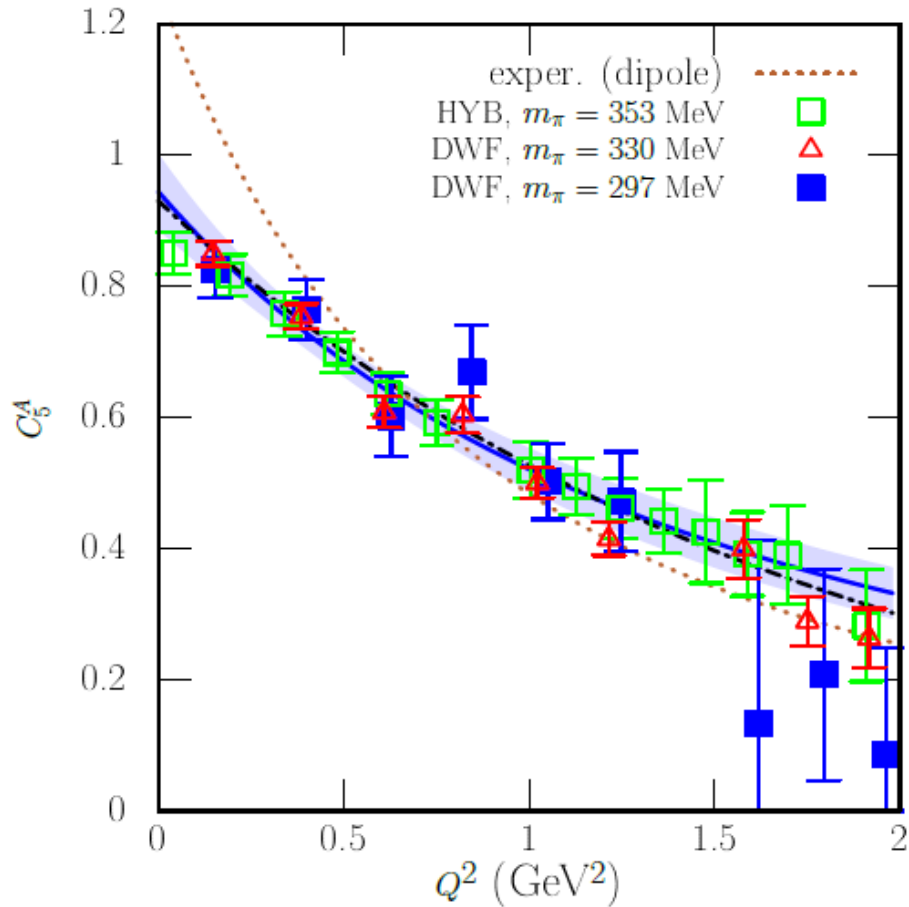
- Fits to ANL and BNL data
  - $C^{A_5}(0) = 1.12 \pm 0.11$ ,  $M_{A\Delta} = 0.95 \pm 0.06$  GeV ← original data (A)
  - $C^{A_5}(0) = 1.14 \pm 0.07$ ,  $M_{A\Delta} = 0.96 \pm 0.07$  GeV ← reanalysis (B)
- For  $C^{A_5}(0)$  :
  - Relative error:  $r_A = 10\%$   $\Rightarrow$   $r_B = 6\%$

However

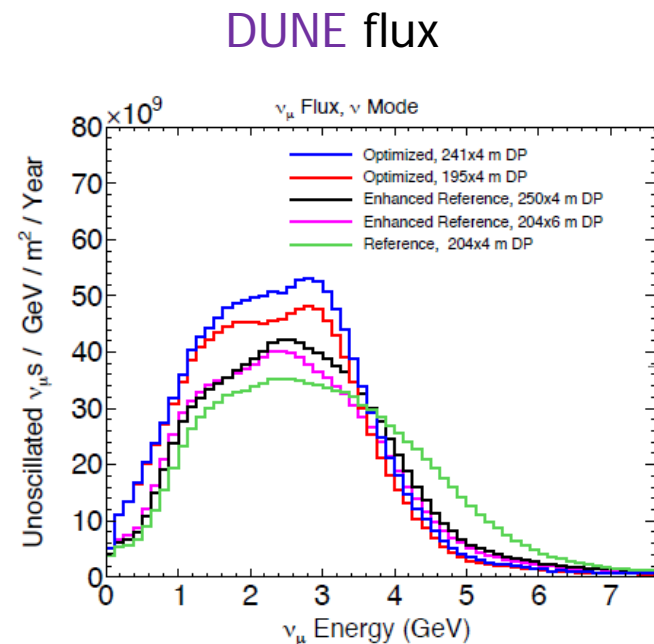
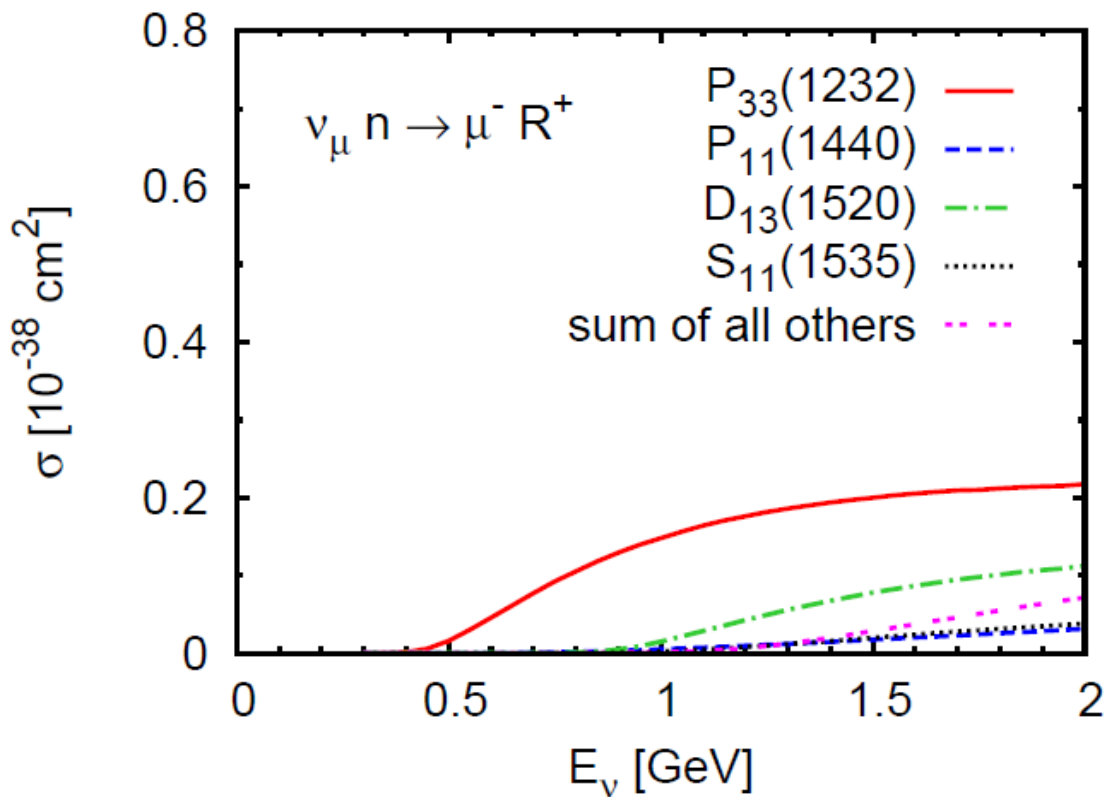
- No improvement in  $M_{A\Delta}$  precision
- ANL and BNL data do not constrain  $C^{A_{3,4}}$  : consistent with zero
- Little (no) sensitivity to heavier baryon resonances
- Modern data: nuclear targets  $\leftrightarrow$  in-medium effects,  $\pi$  FSI
- In the absence of new measurements on nucleons...

# $1\pi$ production on nucleons

- N- $\Delta$  axial form factors in IQCD
- Alexandrou et al., PRD83 (2011)



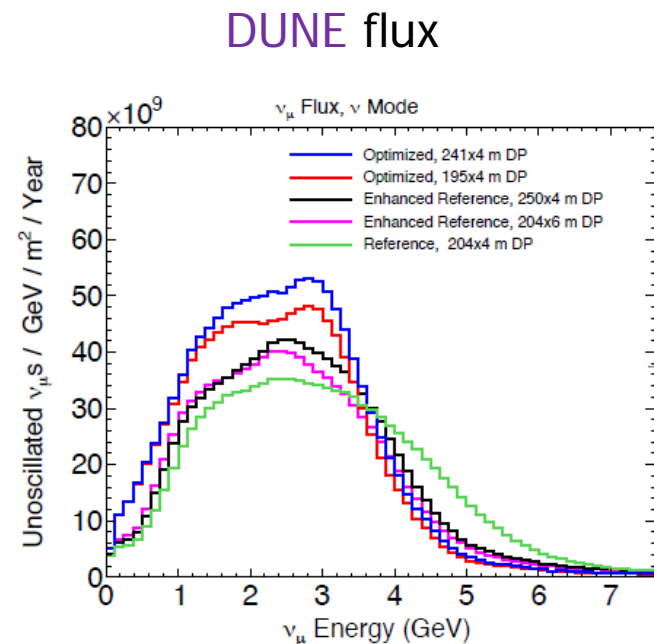
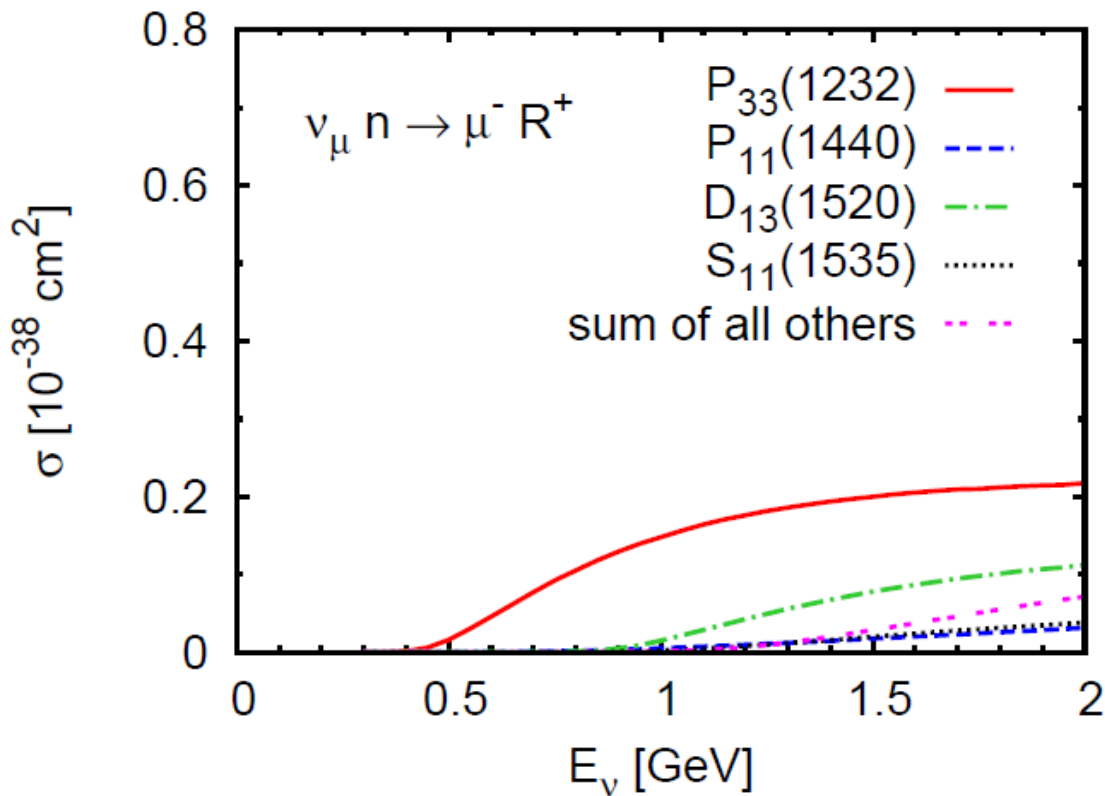
# Inclusive resonance production



T. Leitner, O. Buss, LAR, U. Mosel, PRC 79 (2009)  
 T. Leitner, PhD Thesis, 2009

- At  $E_\nu = 2 \text{ GeV}$ ,  $\text{CCN}^*(1520)/\text{CC}\Delta \sim 0.5$ ,  $\text{CCN}^*(1440,1535)/\text{CC}\Delta \sim 0.22$
- $\text{N}^*(1520)$  is important for  $\nu_l N \rightarrow l N' \pi$

# Inclusive resonance production



T. Leitner, O. Buss, LAR, U. Mosel, PRC 79 (2009)

T. Leitner, PhD Thesis, 2009

■ Baryon resonances contribute to

■ the inclusive  $\nu_l N \rightarrow l X$

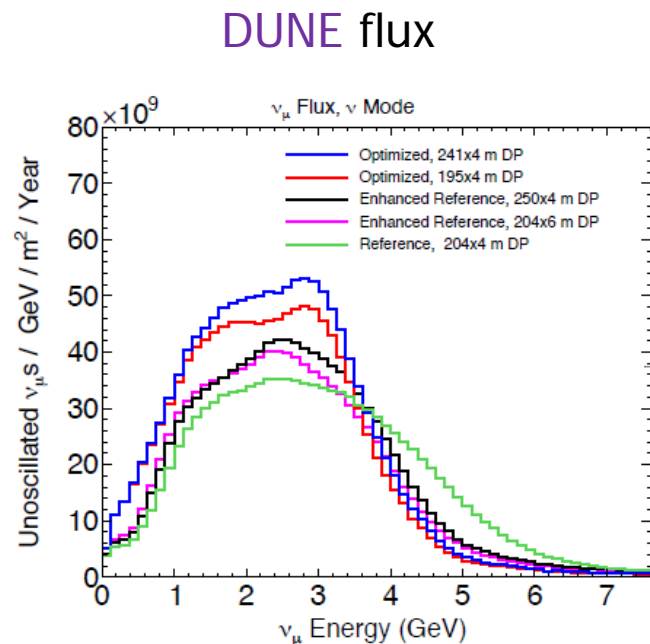
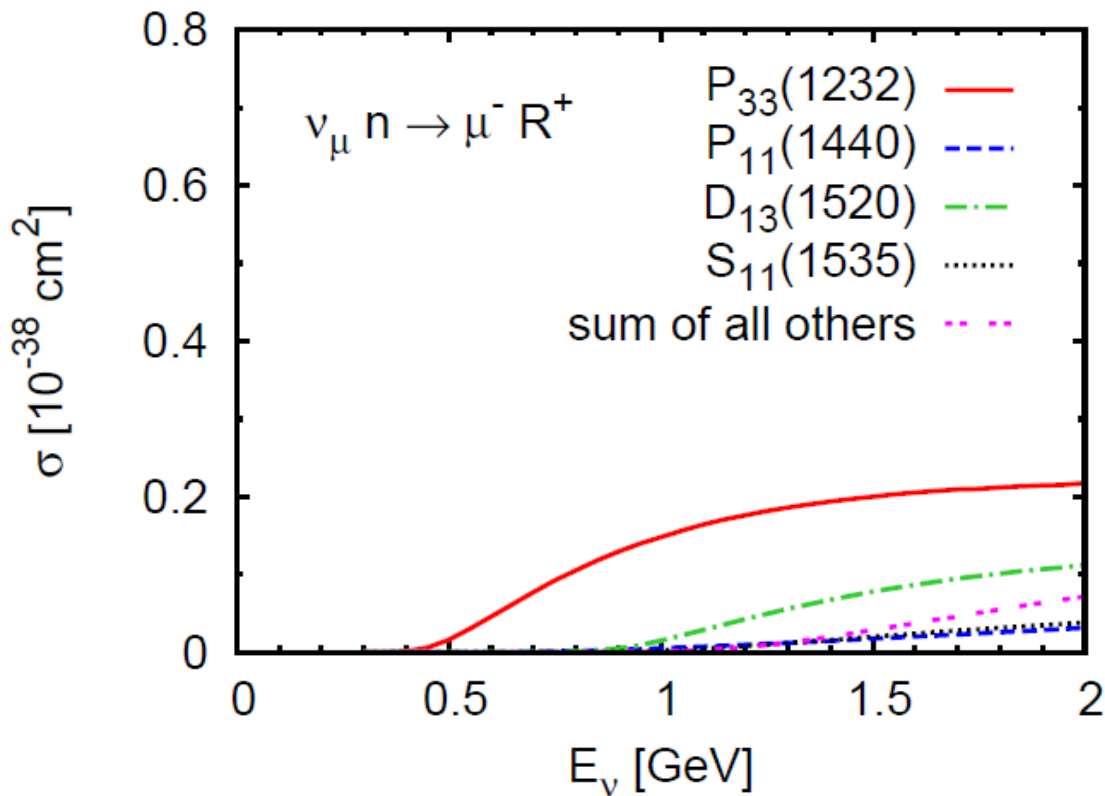
■ several exclusive channels:

$$\nu_l N \rightarrow l N' \gamma$$

$$\nu_l N \rightarrow l N' \eta$$

$$\nu_l N \rightarrow l \Lambda(\Sigma) \bar{K}$$

# Inclusive resonance production



T. Leitner, O. Buss, LAR, U. Mosel, PRC 79 (2009)

T. Leitner, PhD Thesis, 2009

- Educated guess for the axial sector:  $F_A(q^2) = F_A(0) \left(1 - \frac{q^2}{M_A^2}\right)^{-2}$ 
  - **GTR** for leading  $F_A(0)$ ,  $M_A = 1 \text{ GeV}$
  - **Subleading** form factors  $\rightarrow 0$

# Conclusions

- $\nu$  scattering on nucleons and nuclei is relevant for oscillation studies
- Interesting for hadron and nuclear physics
- $\nu$  event generators should be improved/corrected/extended using phenomenological models:
  - consistent with symmetries (in particular ChPT close to threshold)
  - consistent with photon, electron, pion scattering data
- Input/benchmarks from ab initio calculations, including IQCD