Effective
Field
Theory
Gauge
Lattice

Goals of the Focus Group

Andreas S. Kronfeld
Fermilab & IAS TU München
Hans Fischer Senior Fellowship Kick-Off Symposium
26 November 2014

IAS TUM Institute for Advanced Study

Broad Perspective

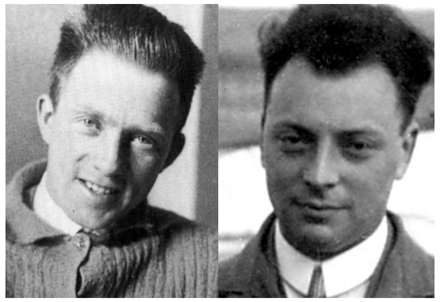
- We are interested in strongly-coupled, relativistic field theories.
- The poster child (Musterbeispiel) is quantum chromodynamics (QCD).
- Two highly successful tools: lattice gauge theory and effective field theory.
- How can these tools be (further) combined to learn more about QCD, and particle physics for which QCD must be understood?
- Magically, relativistic fermions (i.e., $E^2 = \boldsymbol{p}^2 + m^2$) can be found in condensed-matter systems:
    - How can our experience with QCD illuminate these problems?

Outline

- Tools: Lattice Gauge Theory & Effective Field Theory
- Physics:
  - Flavor—bringing out the success of lattice QCD
  - Light-cone physics—without the light cone
  - Optical lattices with gauge symmetries
- Short Stories

LATTICE GAUGE THEORY
FOR BEGINNERS

QFT and a Lattice



- Quantum field theory contains an uncountably infinite number of degrees of freedom—in order to count straight some sort of regulator is needed:

  - *In der Tat kann man den Fall kontinuierlich vieler Freiheitsgrade, wo die Zustandsgrößen Raumfunktionen sind, stets durch Grenzübergang aus dem Fall endlich vieler Freiheitsgrade gewinnen.* Heisenberg, Pauli, *ZPh* **56**, 1 (1929)

  - Indeed, one can always obtain the case of continuously many degrees of freedom, where the state variables are functions of space, through a limit of the case of finitely many degrees or freedom. (*My translation*.)

- Heisenberg & Pauli used a spatial lattice.

- Feynman’s path integral approach to QM discretizes time.

Lattice Gauge Theory

K. Wilson, *PRD* **10** (1974) 2445

- Invented to understand asymptotic freedom without the need for gauge-fixing and ghosts [Wilson, hep-lat/0412043].

- Gauge symmetry on a spacetime lattice:

    - mathematically rigorous definition of QCD functional integrals;

$$\langle \bullet \rangle = \frac{1}{Z} \int \mathcal{D}U \mathcal{D}\psi \mathcal{D}\bar{\psi} \exp\left(-S\right) [\bullet]$$

    - enables theoretical tools of statistical mechanics in quantum field theory and provides a basis for constructive field theory.

- Lowest-order strong coupling expansion demonstrates confinement.

Numerical Lattice QCD

- Nowadays "lattice QCD" usually implies a numerical technique, in which the functional integral is integrated numerically on a computer.

- Big computers:

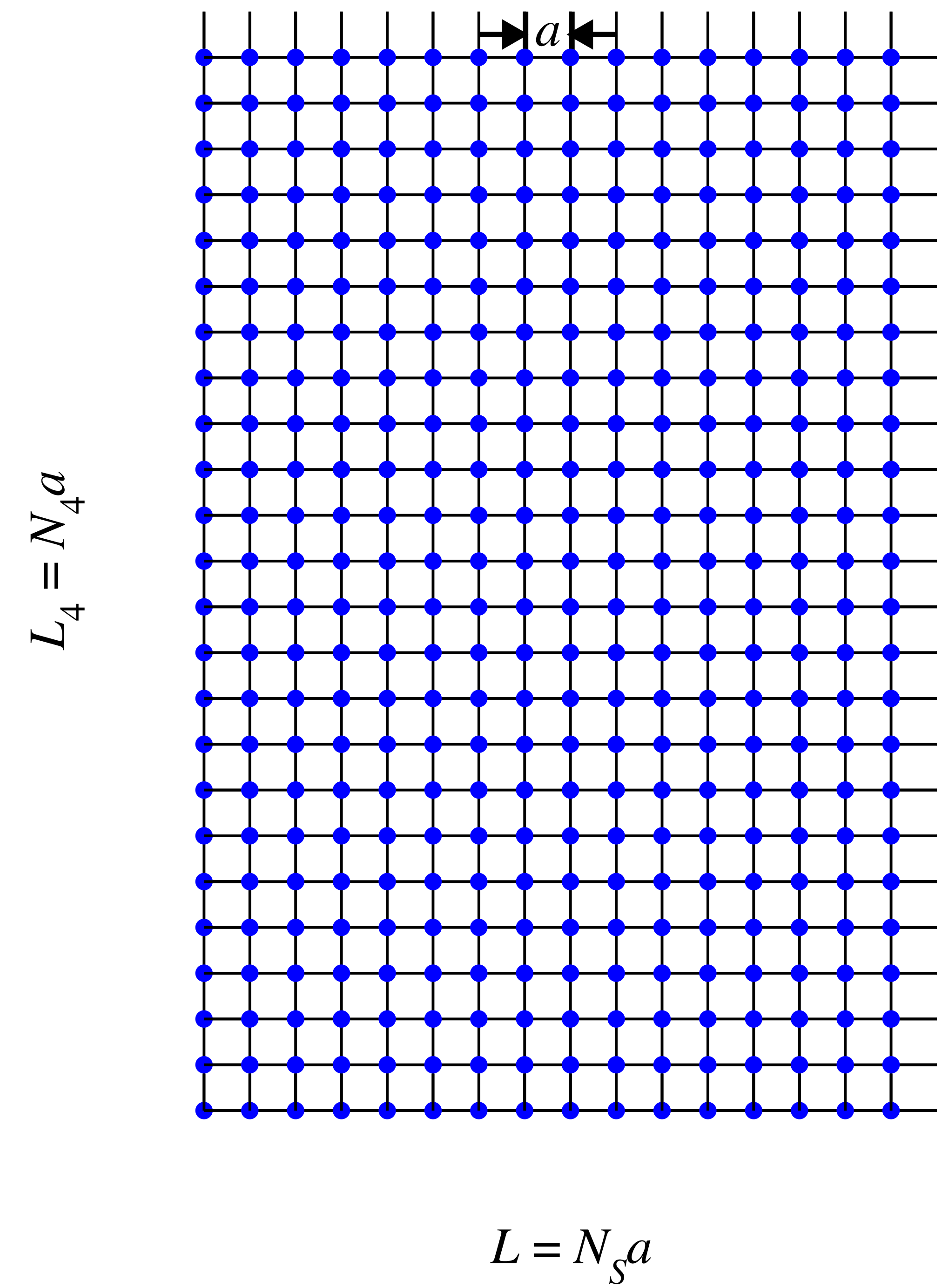
- Some compromises:
  - finite human lifetime ⇒ Wick rotate to Euclidean time: $x^4 = ix^0$;
  - finite memory ⇒ finite space volume & finite time extent;
  - finite CPU power ⇒ light quarks until recently heavier than up and down.

Lattice Gauge Theory

$$\langle \bullet \rangle = \frac{1}{Z} \int \mathcal{D}U \mathcal{D}\psi \mathcal{D}\bar{\psi} \exp\left(-S\right) [\bullet]$$

$$= \frac{1}{Z} \int \mathcal{D}U \ \mathrm{Det}(\not{D} + m) \exp\left(-S_{\mathrm{gauge}}\right) [\bullet']$$

- Infinite continuum: uncountably many d.o.f. (⇒ UV divergences);
- Infinite lattice: countably many; used to define QFT;
- Finite lattice: finite dimension ~ 10^8, so compute integrals numerically.



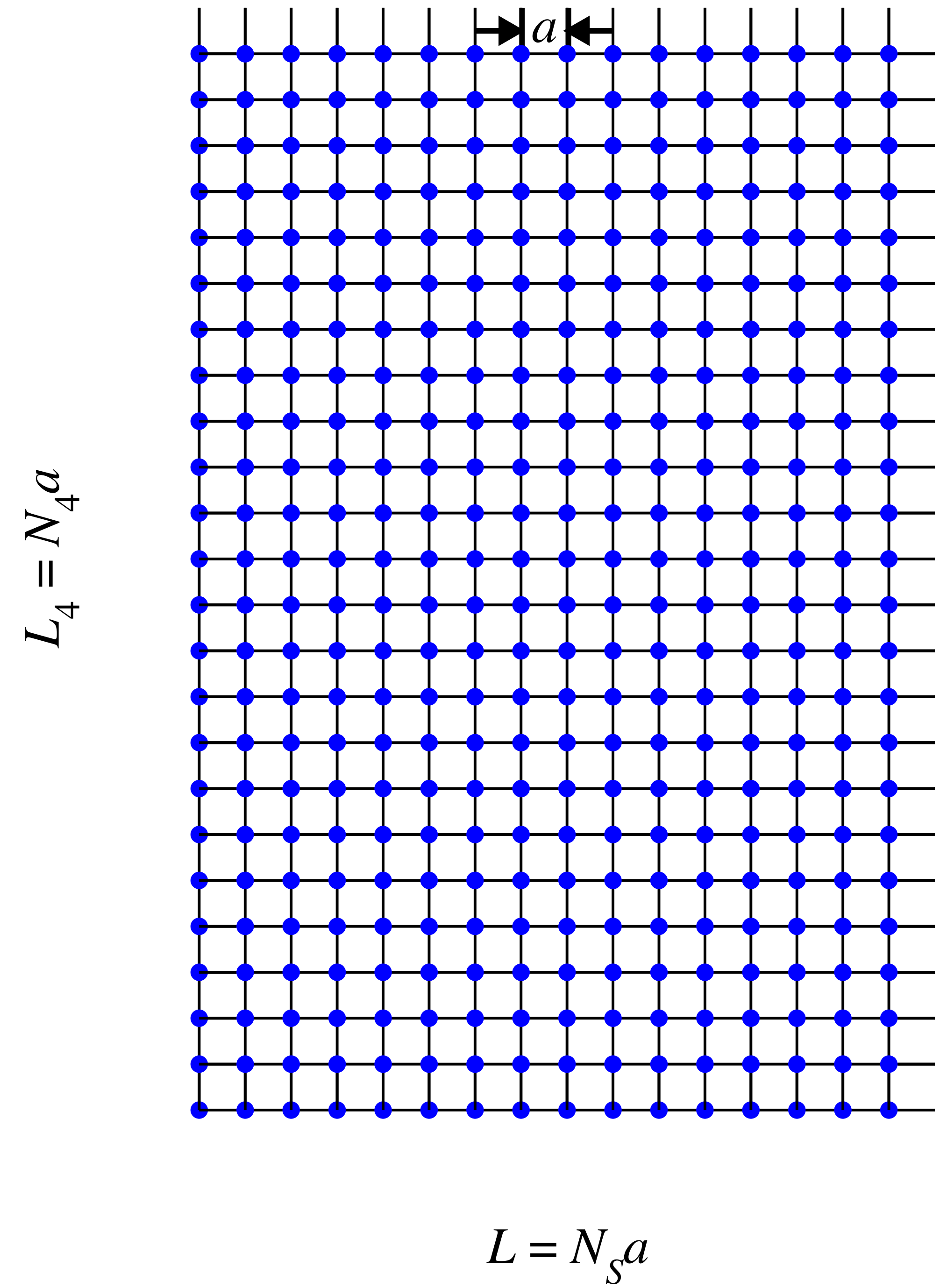
Lattice Gauge Theory

$$\langle \bullet \rangle = \frac{1}{Z} \int \mathcal{D}U \mathcal{D}\psi \mathcal{D}\bar{\psi} \exp\left(-S\right) [\bullet]$$

hand

$$= \frac{1}{Z} \int \mathcal{D}U \ \mathrm{Det}(\not{D} + m) \exp\left(-S_{\mathrm{gauge}}\right) [\bullet']$$

- Infinite continuum: uncountably many d.o.f. (⇒ UV divergences);
- Infinite lattice: countably many; used to define QFT;
- Finite lattice: finite dimension ~ 10^8, so compute integrals numerically.



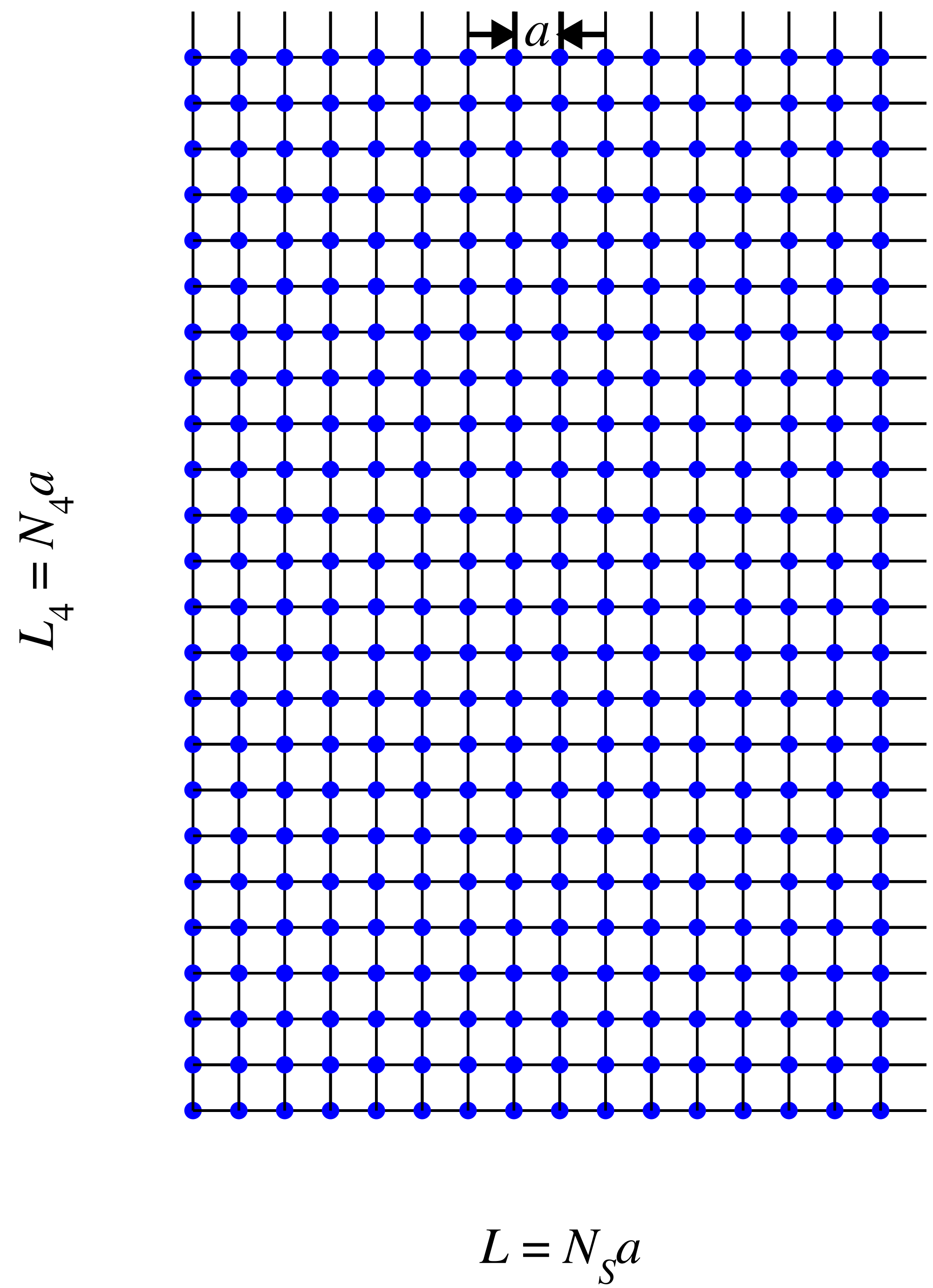
Lattice Gauge Theory

$$\langle \bullet \rangle = \frac{1}{Z} \int \mathcal{D}U \mathcal{D}\psi \mathcal{D}\bar{\psi} \exp(-S) [\bullet]$$

MC hand

$$= \frac{1}{Z} \int \mathcal{D}U \ \mathrm{Det}(\not{D} + m) \exp(-S_{\mathrm{gauge}}) [\bullet']$$

- Infinite continuum: uncountably many d.o.f. (⇒ UV divergences);
- Infinite lattice: countably many; used to define QFT;
- Finite lattice: finite dimension ~ 10^8, so compute integrals numerically.



Some algorithmic issues

e.g., ASK, hep-lat/0205021

- lattice $N_S^3 \times N_4$, spacing a
- memory $\propto N_S^3 N_4 = L_S^3 L_4 / a^4$
- $\tau_g \propto a^{-(4+z)}$, $z = 1$ or 2.
- $\tau_q \propto (m_q a)^{-p}$, $p = 1$ or 2.
- Imaginary time:
  - static quantities
- size $L_S = N_S a$, $L_4 = N_4 a$;
- dimension of spacetime = 4
- critical slowing down
- especially dire with sea quarks
- thermodynamics: $T = 1/N_4 a$

$$\langle \bullet \rangle = \frac{1}{Z} \int \mathcal{D}U \, \mathcal{D}\psi \mathcal{D}\bar{\psi} \exp(-S) \, [\bullet]$$
$$= \mathrm{Tr}\{\bullet \, e^{-\hat{H}/T}\} / \mathrm{Tr}\{e^{-\hat{H}/T}\}$$

- Computationally most demanding part of lattice QCD is $\mathrm{Det}(\not{D}+m)$, which corresponds to the sea quarks.

- First watershed of this century was to include the light sea exactly.

- Nowadays need only to discuss results with
  - $n_f = 2+1$: strange sea + 2 as light as possible for up and down;
  - $n_f = 2+1+1$: add charmed sea to $2+1$.

- In recent (and, hence, coming) years, "as light as possible for up and down" means "as light as up and down in Nature".

- Second watershed of this century.

Correlators Yield Masses & Matrix Elements

- Two-point functions for masses $\pi(t) = \bar{\psi}_u \gamma_5 S \psi_d$:

$$\langle \pi(t)\pi^\dagger(0)\rangle = \sum_n |\langle 0|\hat{\pi}|\pi_n\rangle|^2 \exp(-m_{\pi_n} t)$$

- Two-point functions for decay constants:

$$\langle J(t)\pi^\dagger(0)\rangle = \sum_n \langle 0|\hat{J}|\pi_n\rangle\langle \pi_n|\hat{\pi}^\dagger|0\rangle \exp(-m_{\pi_n} t)$$

- Three-point functions for form factors, mixing:

$$\langle \pi(t)J(u)B^\dagger(0)\rangle = \sum_{mn} \langle 0|\hat{\pi}|\pi_m\rangle\langle \pi_n|\hat{J}|B_m\rangle\langle B_m|\hat{B}^\dagger|0\rangle \times \exp[-m_{\pi_n}(t-u) - m_{B_m} u]$$

- LHS needs supercomputers; RHS needs students, postdocs, junior faculty.

The QCD Lagrangian

H. Fritzsch, M. Gell-Mann, H. Leutwyler, *PLB* **47** (1973) 365

- SU(3) gauge symmetry and $1 + n_f + 1$ parameters:

$$
\begin{aligned}
\mathcal{L}_{\mathrm{QCD}} &= \frac{1}{g_0^2}\,\mathrm{tr}[F_{\mu\nu}F^{\mu\nu}] \\
&- \sum_f \bar{\psi}_f(\not{D} + m_f)\psi_f \\
&+ \frac{i\theta}{32\pi^2}\varepsilon^{\mu\nu\rho\sigma}\,\mathrm{tr}[F_{\mu\nu}F_{\rho\sigma}]
\end{aligned}
$$

- Observable CP violation $\propto \vartheta = \theta - \arg\det m_f$ (if all masses nonvanishing):
  - neutron electric-dipole moment sets limit $\vartheta \lesssim 10^{-11}$;
  - bafflingly implausible cancellation called the strong CP problem.

The QCD Lagrangian

H. Fritzsch, M. Gell-Mann, H. Leutwyler, *PLB* **47** (1973) 365

- SU(3) gauge symmetry and $1 + n_f + 1$ parameters:

$$\begin{aligned} \mathcal{L}_{\mathrm{QCD}} &= \frac{1}{g_0^2}\mathrm{tr}[F_{\mu\nu}F^{\mu\nu}] && r_1 \text{ or } m_\Omega \text{ or } \Upsilon(2S\text{-}1S), \ldots. \\ &- \sum_f \bar{\psi}_f(\not{D}+m_f)\psi_f && m_\pi, m_K, m_{J/\psi}, m_\Upsilon, \ldots. \\ &+ \frac{i\theta}{32\pi^2}\varepsilon^{\mu\nu\rho\sigma}\mathrm{tr}[F_{\mu\nu}F_{\rho\sigma}] && \theta = 0. \end{aligned}$$

- Observable CP violation $\propto \vartheta = \theta - \arg\det m_f$ (if all masses nonvanishing):
  - neutron electric-dipole moment sets limit $\vartheta \lesssim 10^{-11}$;
  - bafflingly implausible cancellation called the strong CP problem.

Numerical Lattice Gauge Theory

- The lattice provides a UV cutoff; a finite volume provides an IR cutoff; a finite Euclidean time leads to a nonzero temperature.
- Write a random number generator to create lattice gauge fields distributed with the weight of the functional integral.
- Fit correlations functions to get masses and matrix elements.
- Repeat several times while varying bare gauge coupling and bare masses.
- Find a trajectory with constant pion, kaon, D_s, B_s, masses (one for each quark) in dimensionless but physical units and obtain the continuum limit.
- Convert units to MeV.

Numerical Lattice Gauge Theory

- The lattice provides a UV cutoff; a finite volume provides an IR cutoff; a finite Euclidean time leads to a nonzero temperature.
- Write a random number generator to create lattice gauge fields distributed with the weight of the functional integral.
- Fit correlations functions to get masses and matrix elements.
- Repeat several times while varying bare gauge coupling and bare masses.
- Find ... quark) in d...

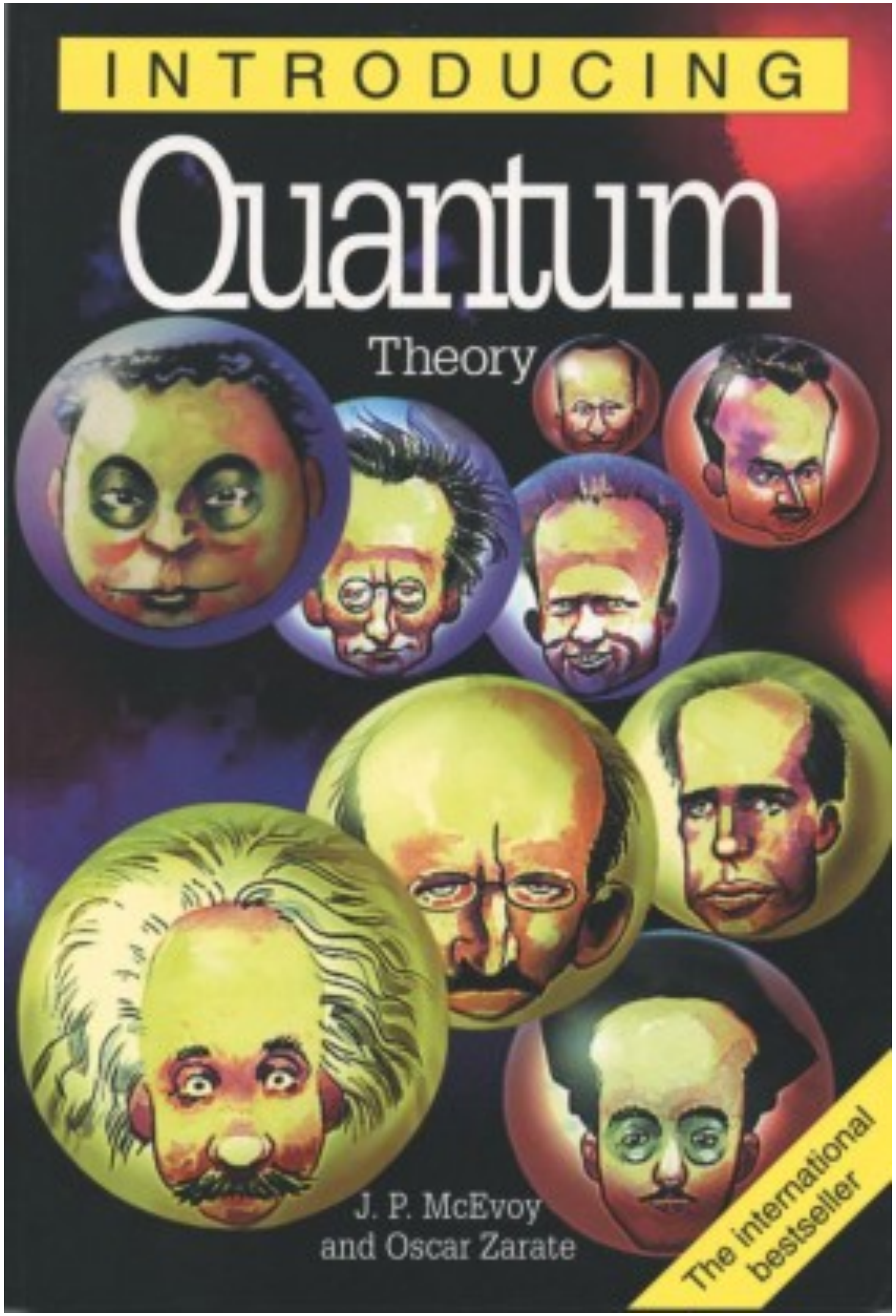
requires wisdom and effective field theory

- Convert units to MeV.

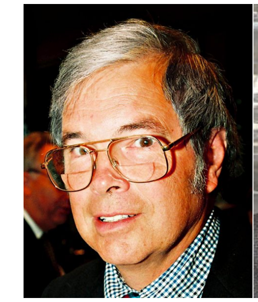
INTRODUCING

Effective

Field Theory



Effective Field Theories




- An implementation of the renormalization group:
  - separating different length scales (equivalently energy scales);
  - can "integrate out" short-distance physics, lumping those effects into coefficient functions (Wilson);
  - can use physical reasoning to deduce relevant long-distance degrees of freedom, and parametrize with a general Lagrangian (Weinberg).
- Separation of scales is the key: can use the most appropriate theoretical tool at each length scale:
  - *e.g.*, lattice gauge theory for Λ_{QCD}, perturbative EFT for shorter distances.

Apt Examples

- Heavy-quark effective theory for hadrons with a single heavy quark: m_Q, Λ_{QCD}.
- Non-relativistic QCD for quarkonium: m_Q, m_Qv, m_Qv^2, m_Qv^4, ..., $\alpha_s \sim v$.
  - HQET & NRQCD "share" the same Lagrangian, but the physics requires different power counting.
- Potential NRQCD (and related EFTs), when m_Qv, m_Qv^2, ... lie at short enough distances for perturbative QCD to be reliable.
- Soft-collinear effective theory for highly energetic (jets of) particles: not yet formulated in a "Euclid friendly" way, so no connection to lattice QCD yet.

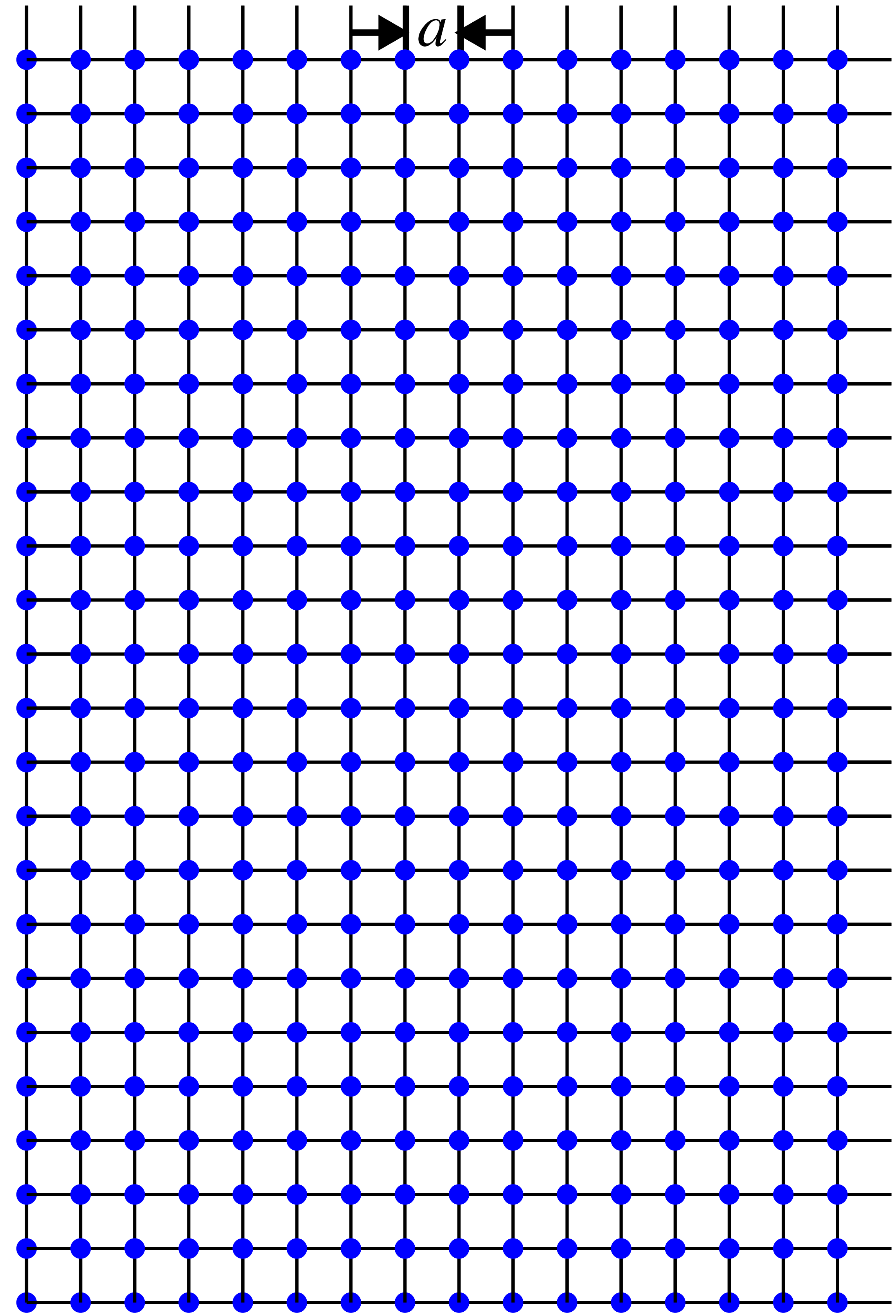
Effective

Field

Theory

Gauge

Lattice



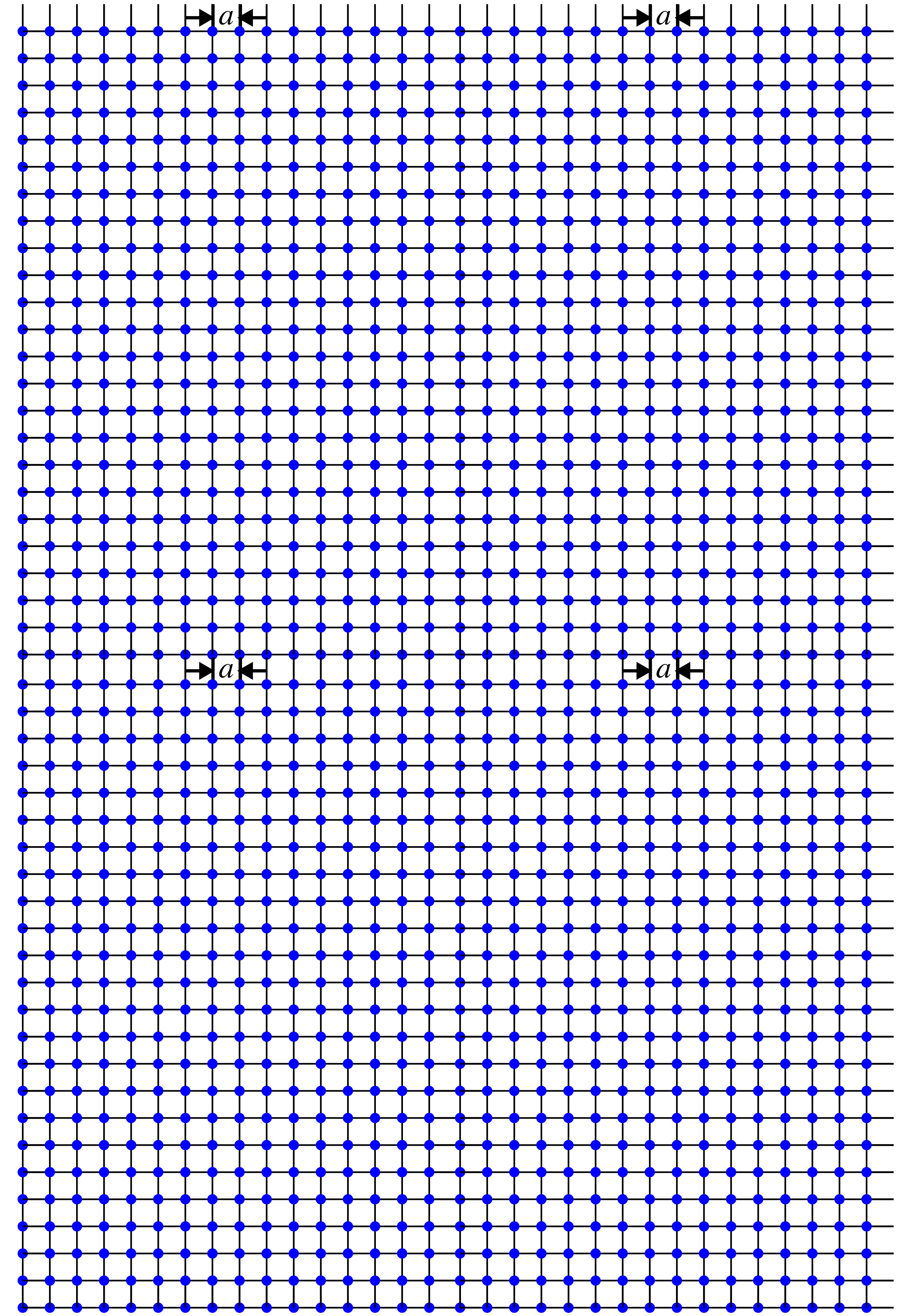
Effective

Field

Theory

Gauge

Lattice



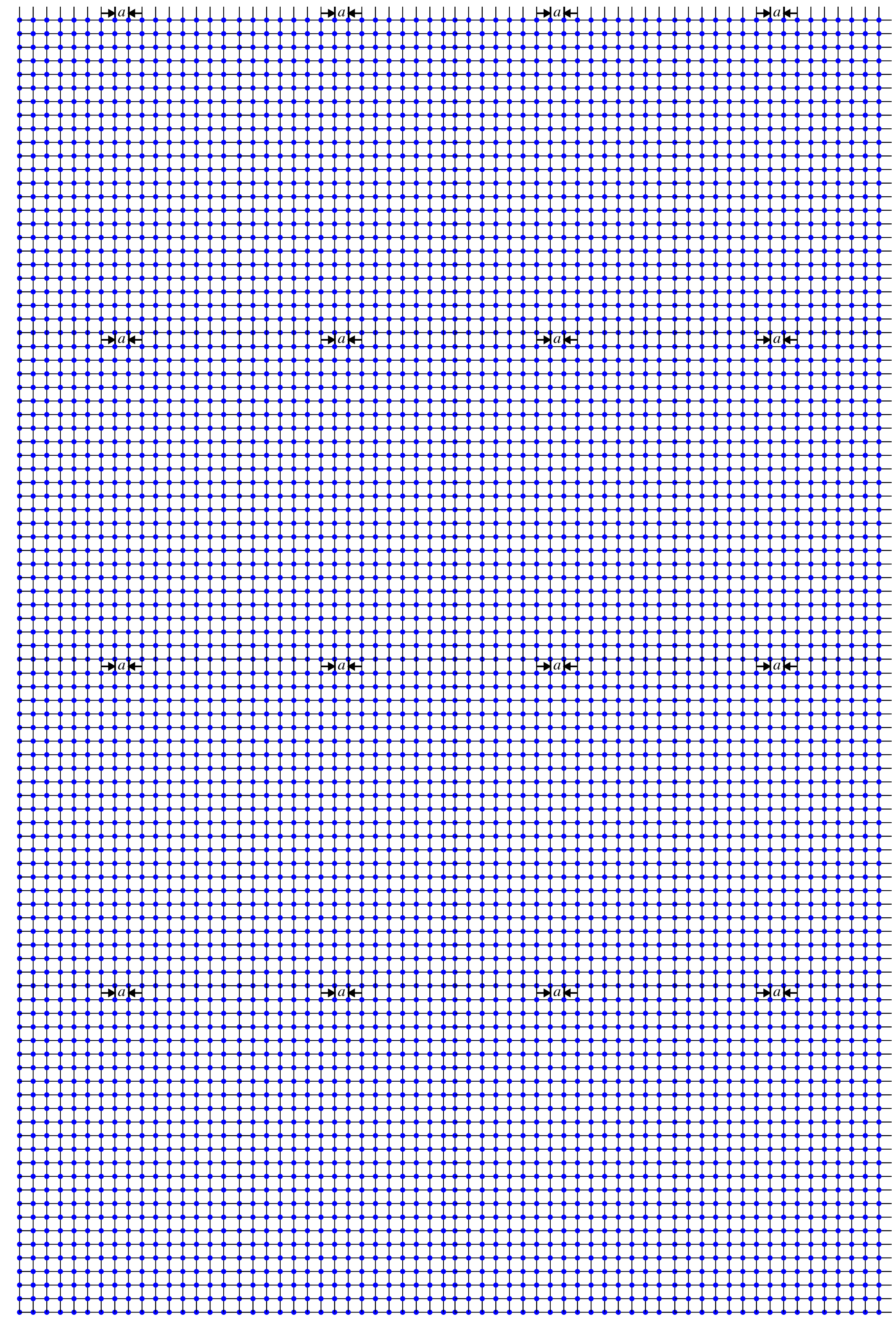
Effective

Field

Theory

Gauge

Lattice



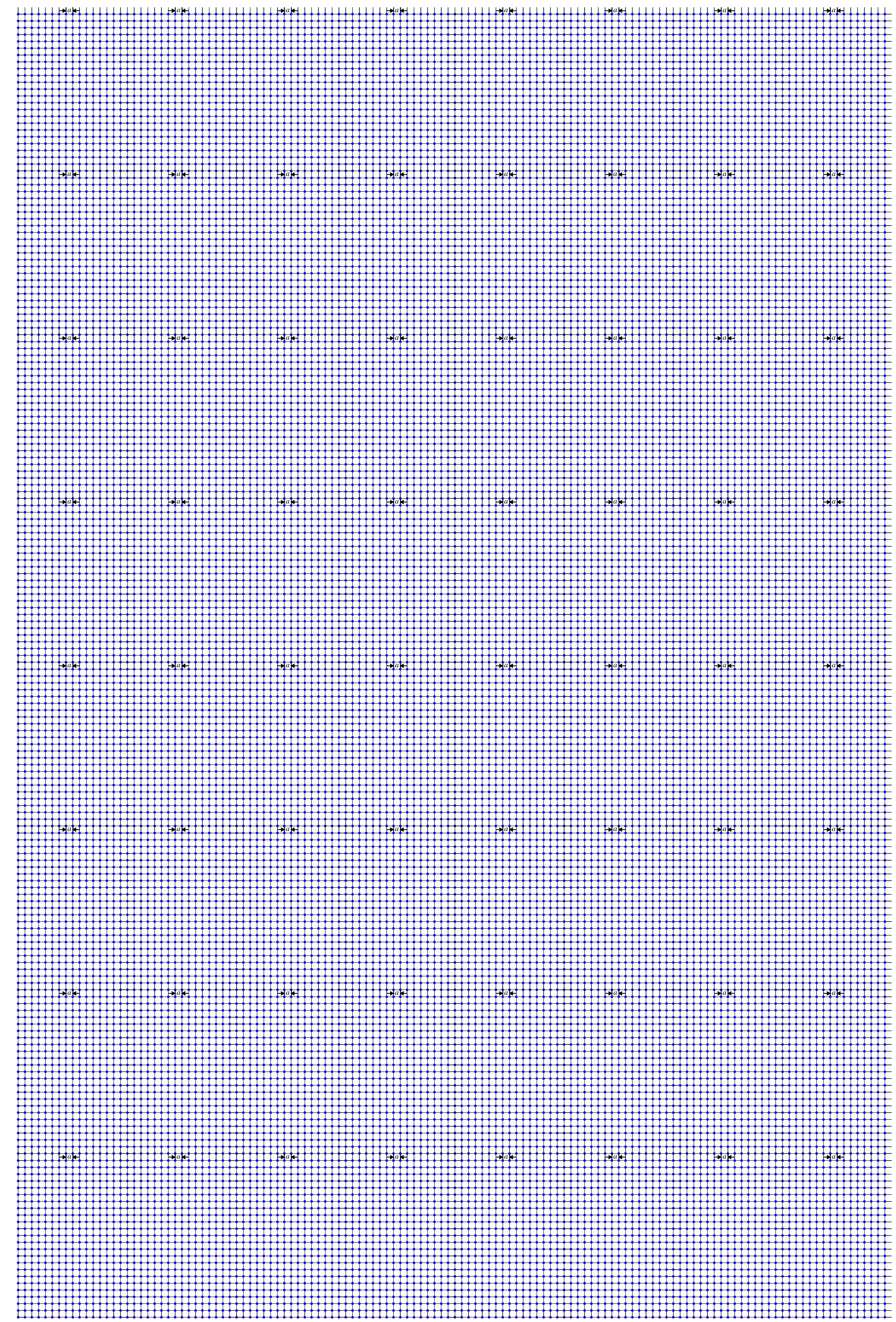
Effective

Field

Theory

Gauge

Lattice



Effective Field Theory

- The lattice provides a UV cutoff: Symanzik effective field theory.
- The finite volume provides an IR cutoff: effective field theory in a box:
  - loop integrals become finite sums;
  - these effects are either v. small or v. useful (absorptive parts).
- Sometimes the light quarks aren't light enough: chiral perturbation theory:
  - replace the computer's pion cloud with Nature's.
- Sometimes heavy-quark masses have $m_Q a \approx 1$: HQET or NRQCD.

Validating the Paradigm

How to validate a method …

- Quantum chromodynamics with UV and IR cutoffs, with extrapolations guided by renormalization & effective field theory ideas.

- Monte Carlo codes tested numerous ways (unit tests; reproducibility).

- Theoretical checks of programs, *e.g.*, Dirac eigenvalues satisfy various low-energy theorems.

- Hadron spectrum and other postdictions.

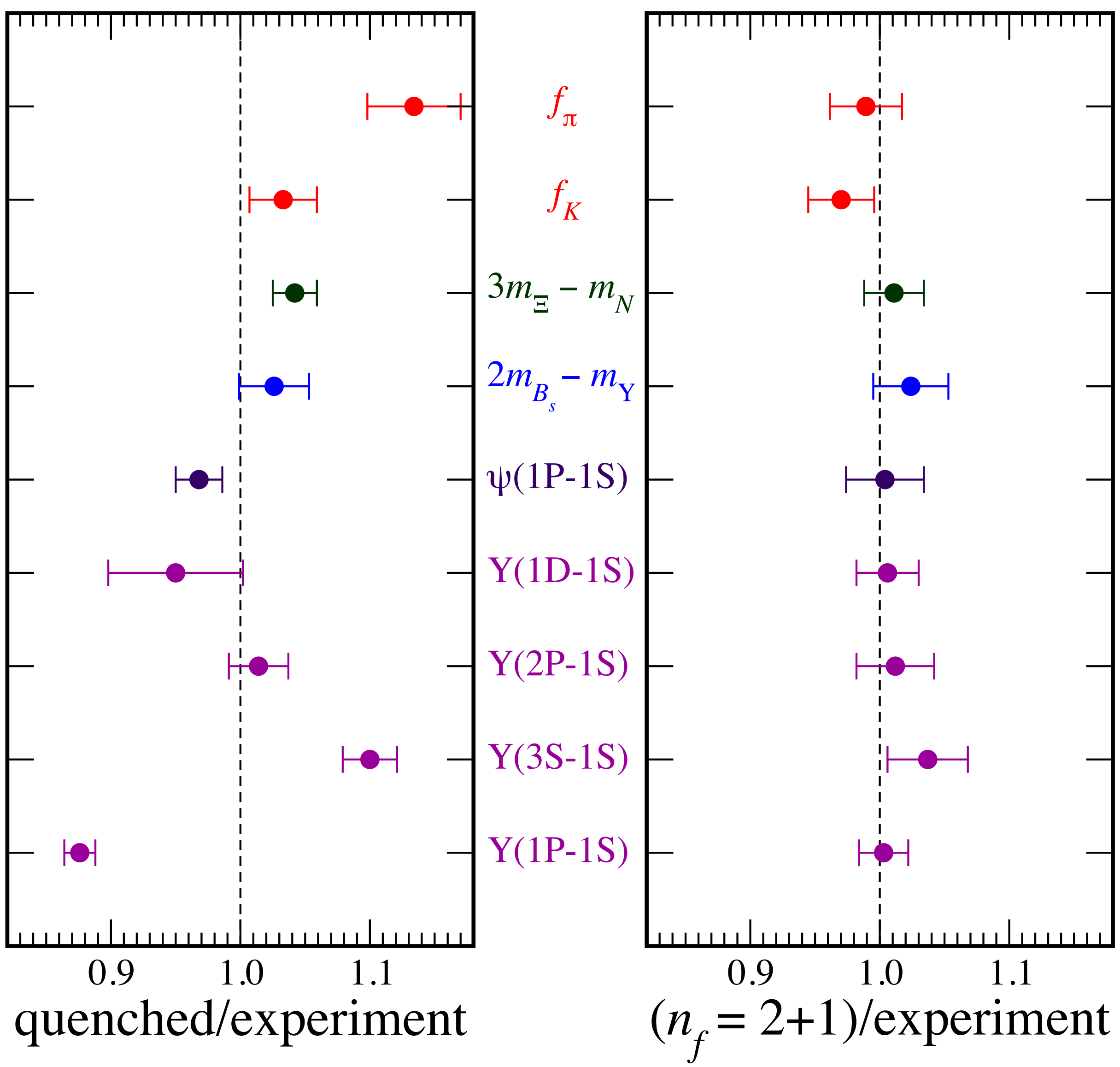
as much
a test of
practitioners

- Genuine predictions: compute something not yet well measured:

    - decay constant f_D, $D \to Kl\nu$ form factor, B_c and η_b masses, ….

Postdictions

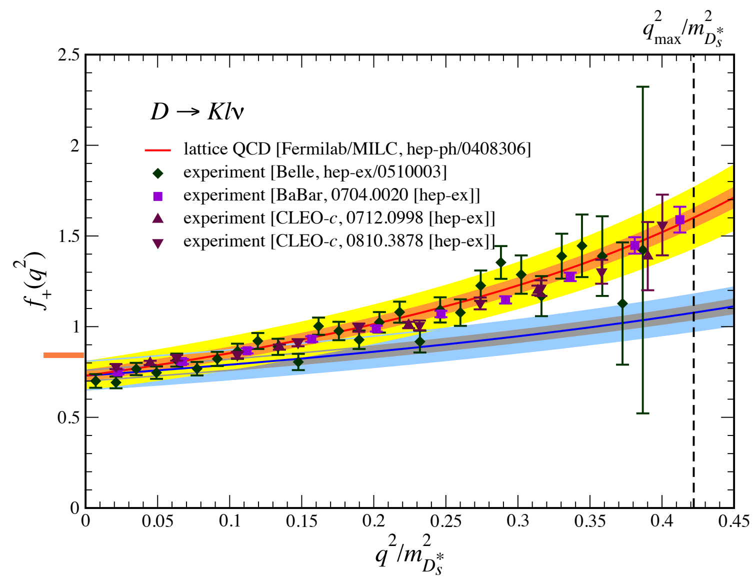
HPQCD, MILC, Fermilab Lattice, hep-lat/0304004

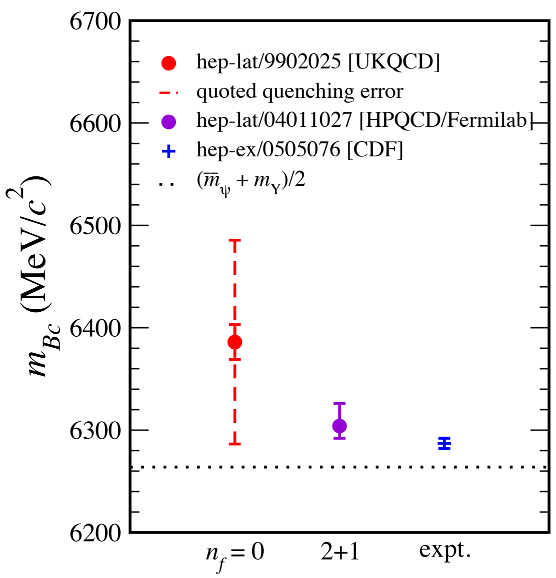


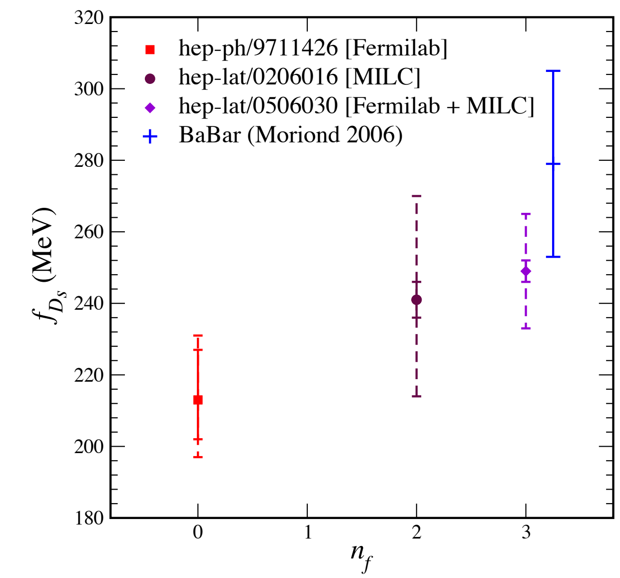
- $a = 0.12$ & 0.09 fm;
- $O(a^2)$ improved: asqtad;
- FAT7 smearing;
- $2m_l < m_q < m_s$;
- π, K, Υ(2S-1S) input.

Predictions

Fermilab Lattice, MILC, HPQCD, hep-lat/0607011







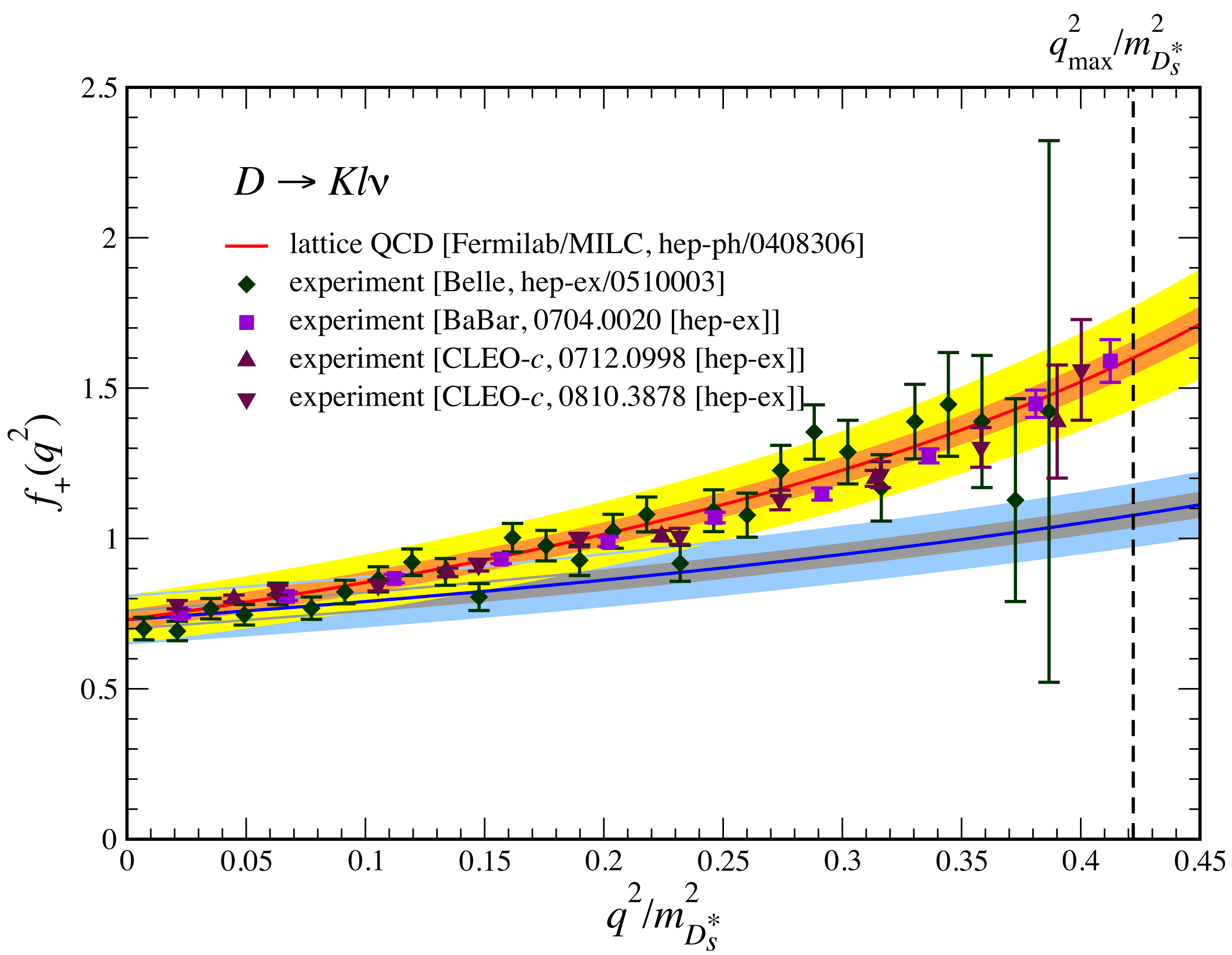
- Semileptonic form factor for $D \to Kl\nu$: hep-ph/0408306—updates: arXiv:1008.4562 (normalization), arXiv:1305.1462 (shape);
- Charmed-meson decay constants: hep-lat/0506030—updates below;
- Mass of B_c meson: hep-lat/0411027—updates: arXiv:0909.4462, arXiv:1010.3848 ($M_{B_c^*} = 6.330(9)$ GeV), arXiv:1207.5149 ($M_{B_c'} = 6.89(2)$ GeV).

An Old Result

- FOCUS, Belle, BaBar, and CLEO validated the prediction of 2004 lattice QCD.

- Take $|V_{cs}|$ from CKM unitarity.

- Similar story for $D \to \pi l \nu$.



A New Result

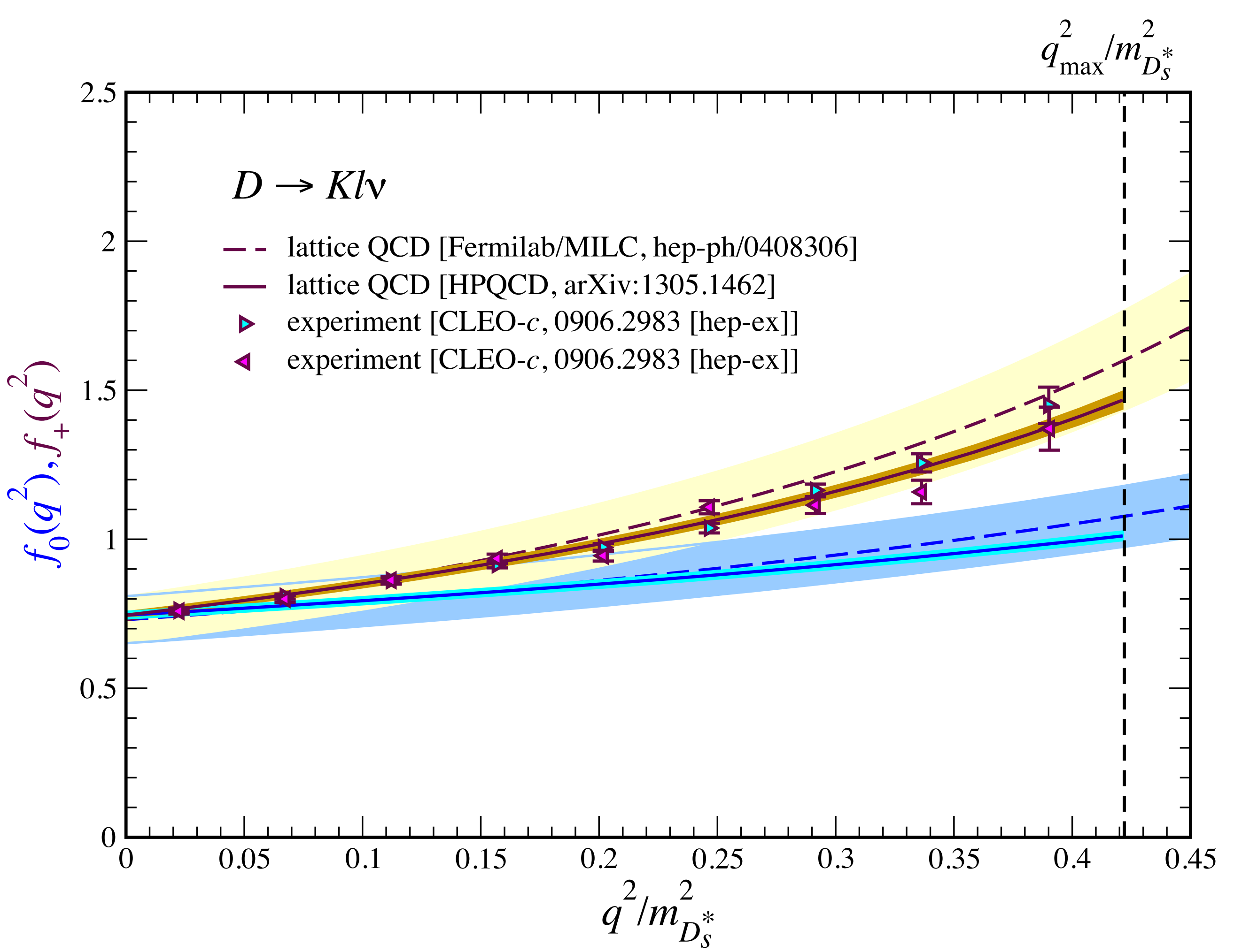
- The most precise experimental data (from CLEO-*c*) are on the lower edge of the 2004 result.

- But today's lattice QCD is more precise than before.

- A new calculation [arXiv:1305.1462, HPQCD] lands in the same place.

- Rather than using CKM as a check, it is now used to determine $|V_{cs}|$.

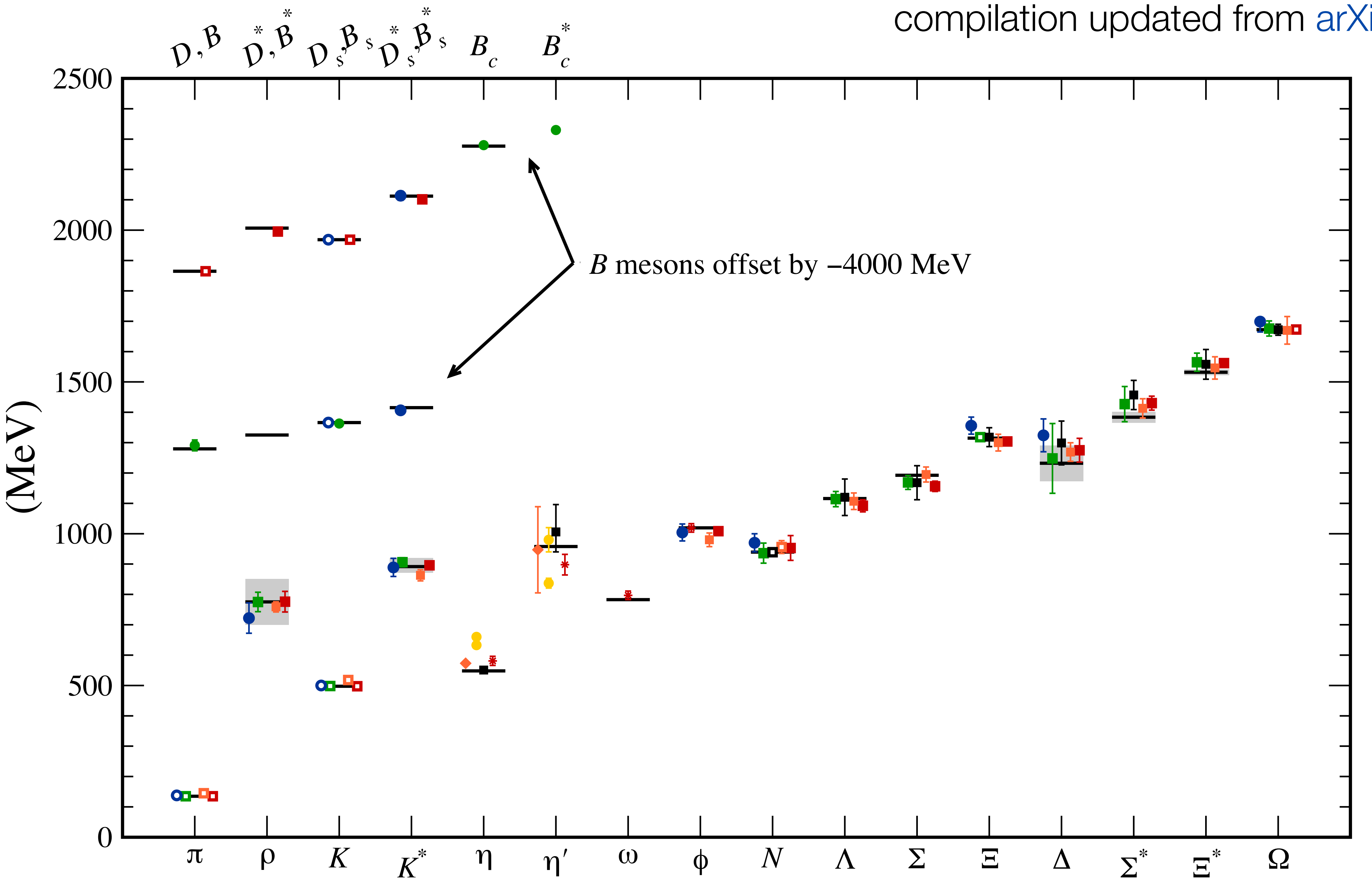
- Follows a procedure like that used to determine $|V_{ub}|$ from $B \to \pi l\nu$.



QCD Hadron Spectrum

π…Ω: BMW, MILC, PACS-CS, QCDSF, ETM (2+1+1);
η-η′: RBC, UKQCD, Hadron Spectrum (ω);
D, *B*: Fermilab, HPQCD, Mohler&Woloshyn

compilation updated from arXiv:1203.1204



numerous quarkonium omitted

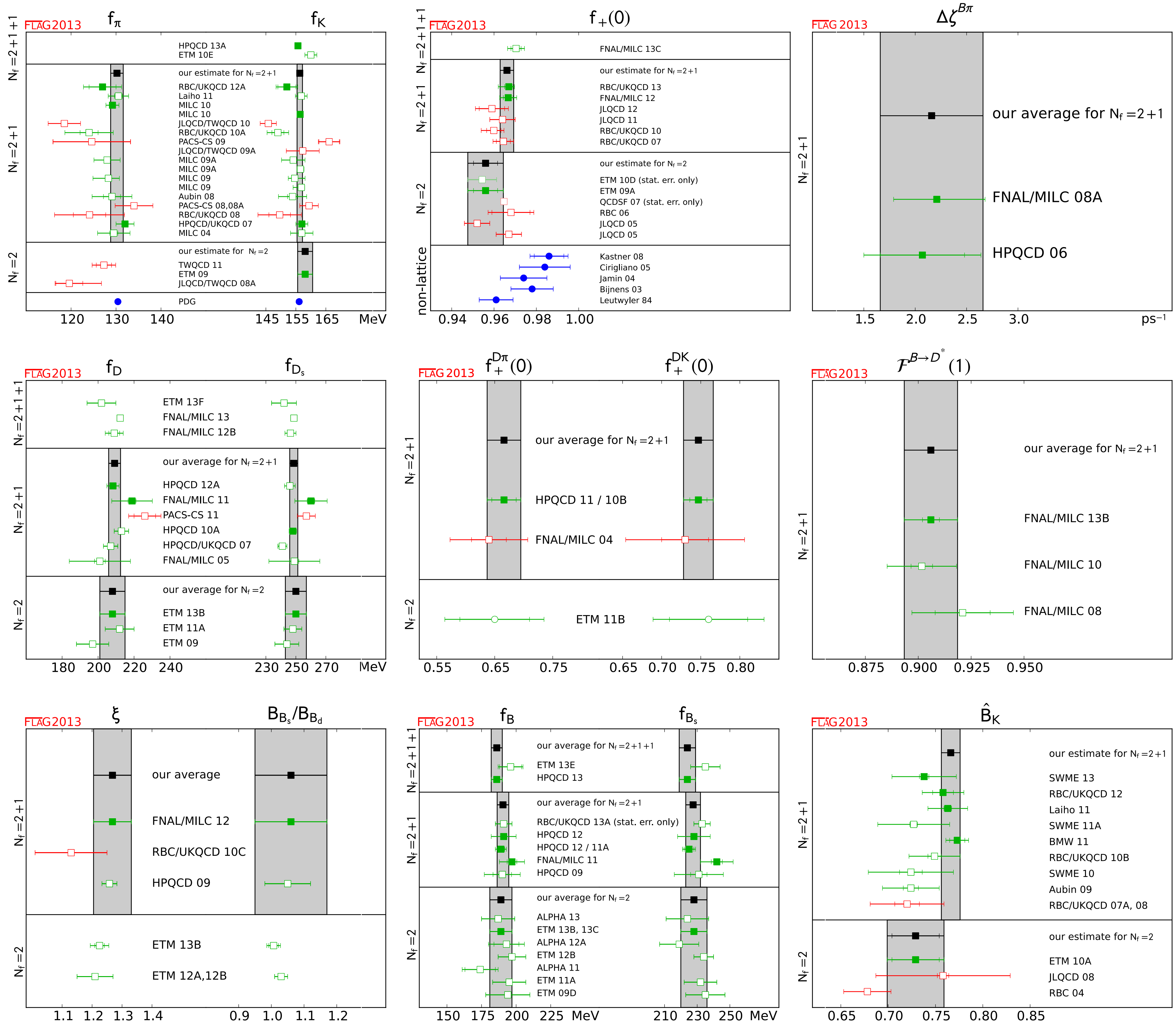
Flavor Physics

CKM and Lattice QCD

- Gold-plated quantities available to (over)determine CKM matrix.
- Further matrix elements for flavor-changing neutral currents—
  - which arise in many extensions of the Standard Model.
- Flavor Lattice Averaging Group FLAG 2013 (Flavour Lattice Averaging Group):
  - self-selected group drawn from most major lattice QCD collaborations;
  - sets quality criteria and produces averages of quantities germane to CKM;
  - compare & contrast to the PDG perhaps 30 years ago.

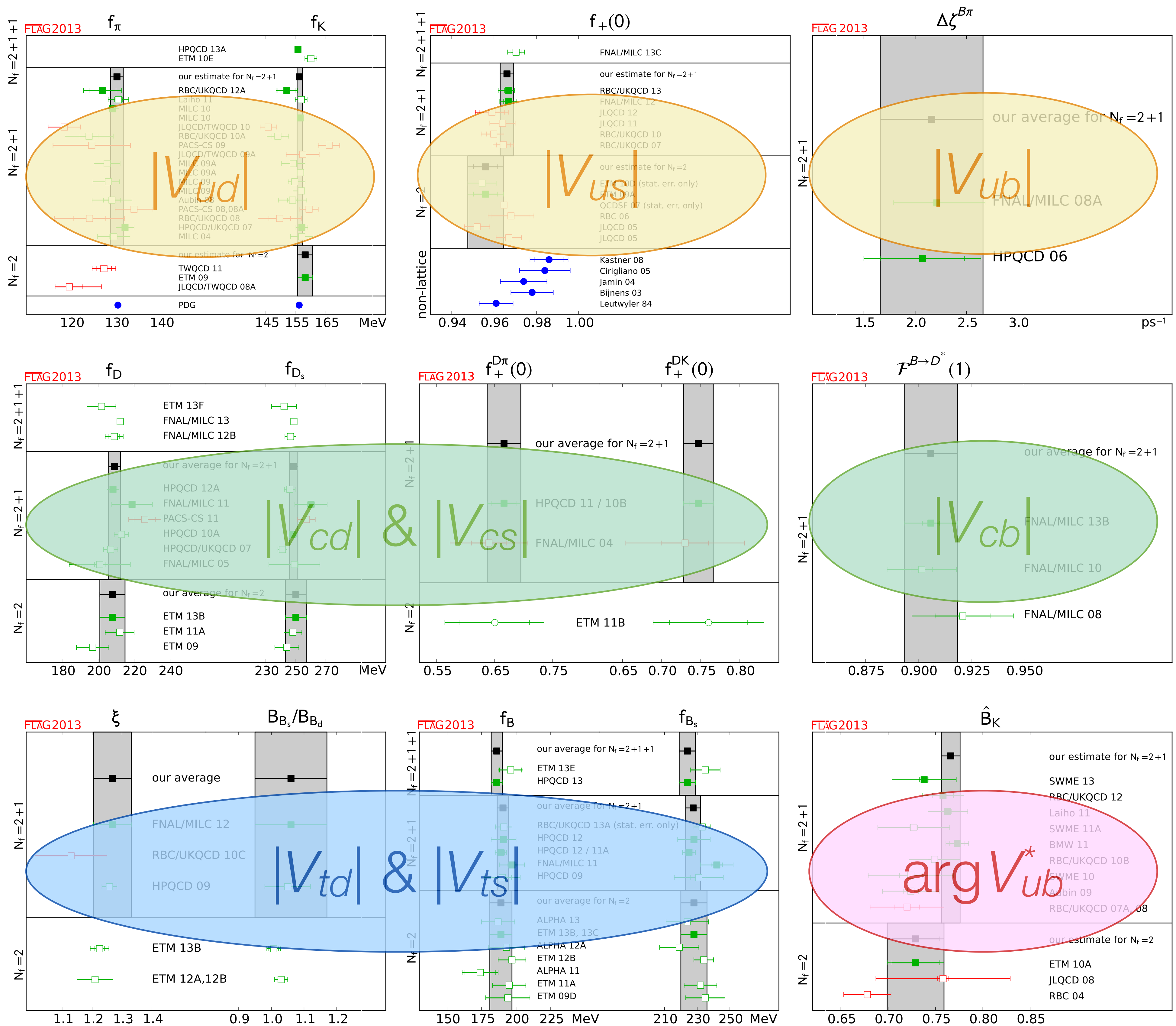
FLAG 2013

Flavour Lattice Averaging Group

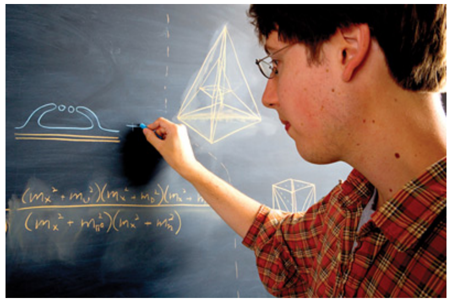


FLAG 2013

Flavour Lattice Averaging Group



Semileptonic $B \to D^* l\nu$ for $|V_{cb}|$



- Like $|V_{us}|$, $|V_{cb}|$ appears everywhere, *e.g.*, in FCNC rare kaon decays.

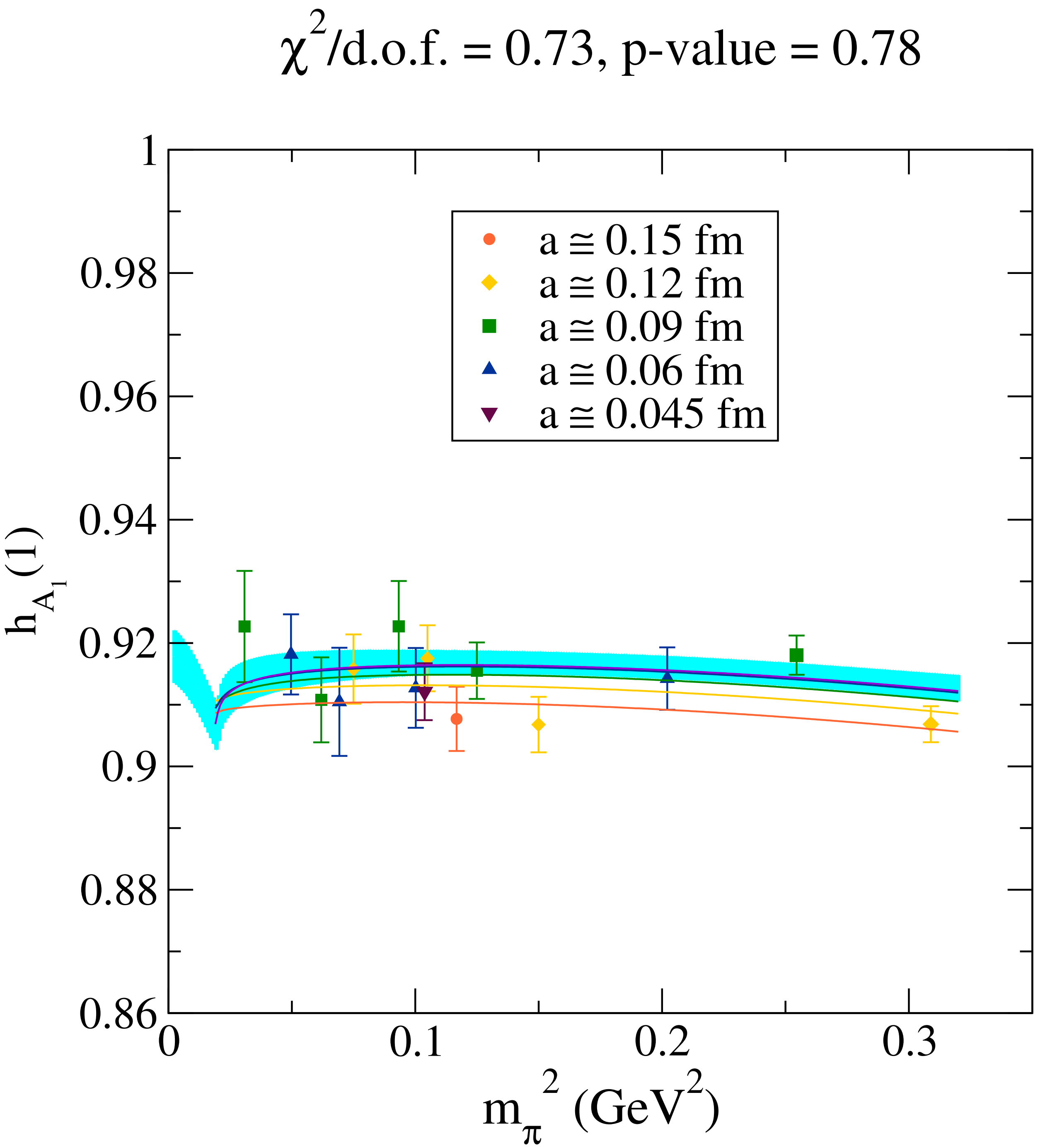
- We find

$$\mathscr{F}(1) = 0.906 \pm 0.004 \pm 0.012$$

or

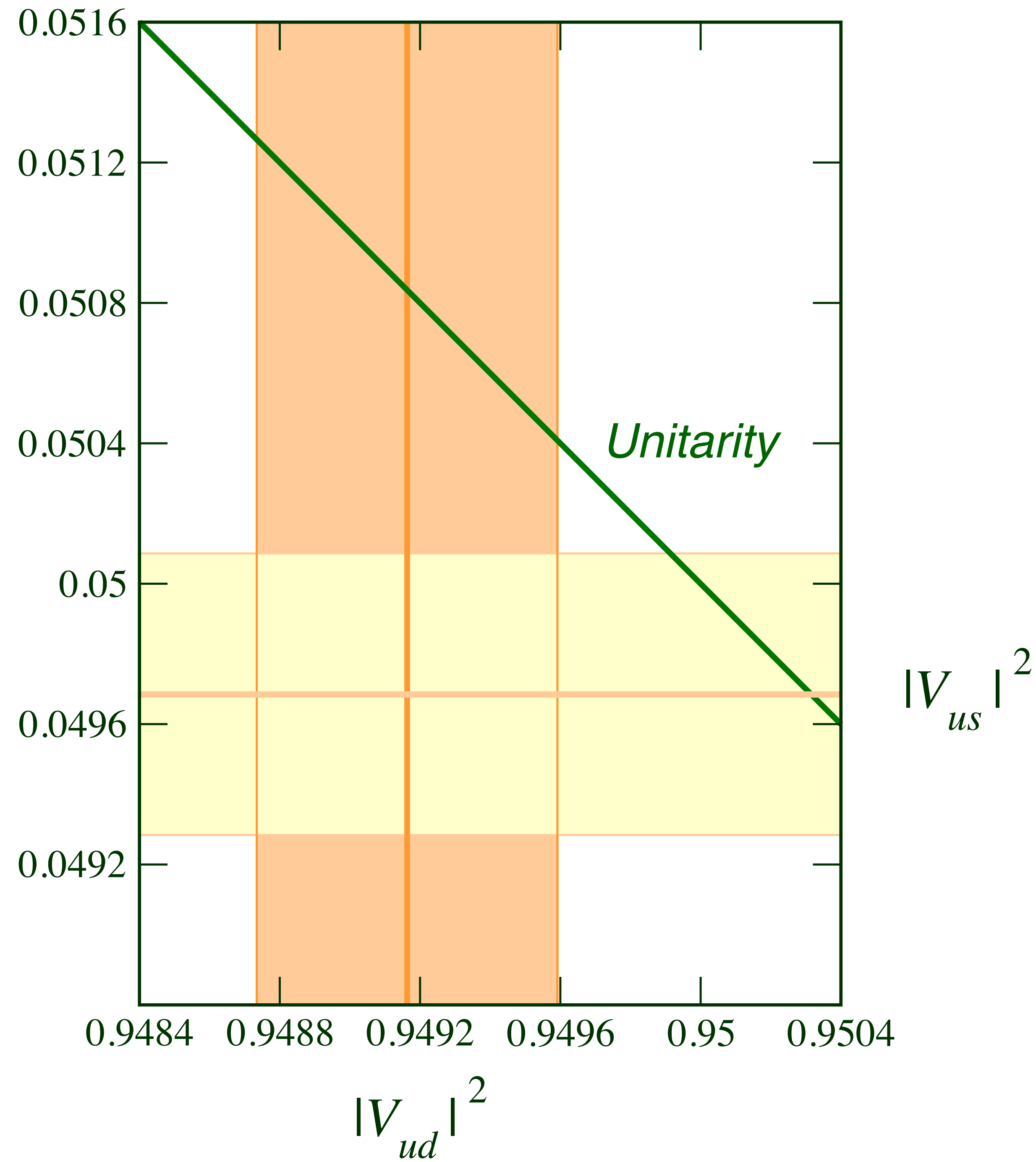
$$10^3 |V_{cb}| = 39.04 \pm 0.49_{\text{expt}} \pm 0.53_{\text{QCD}} \pm 0.19_{\text{QED}}$$

- QCD error as small as expt; as small as inclusive-decay method.



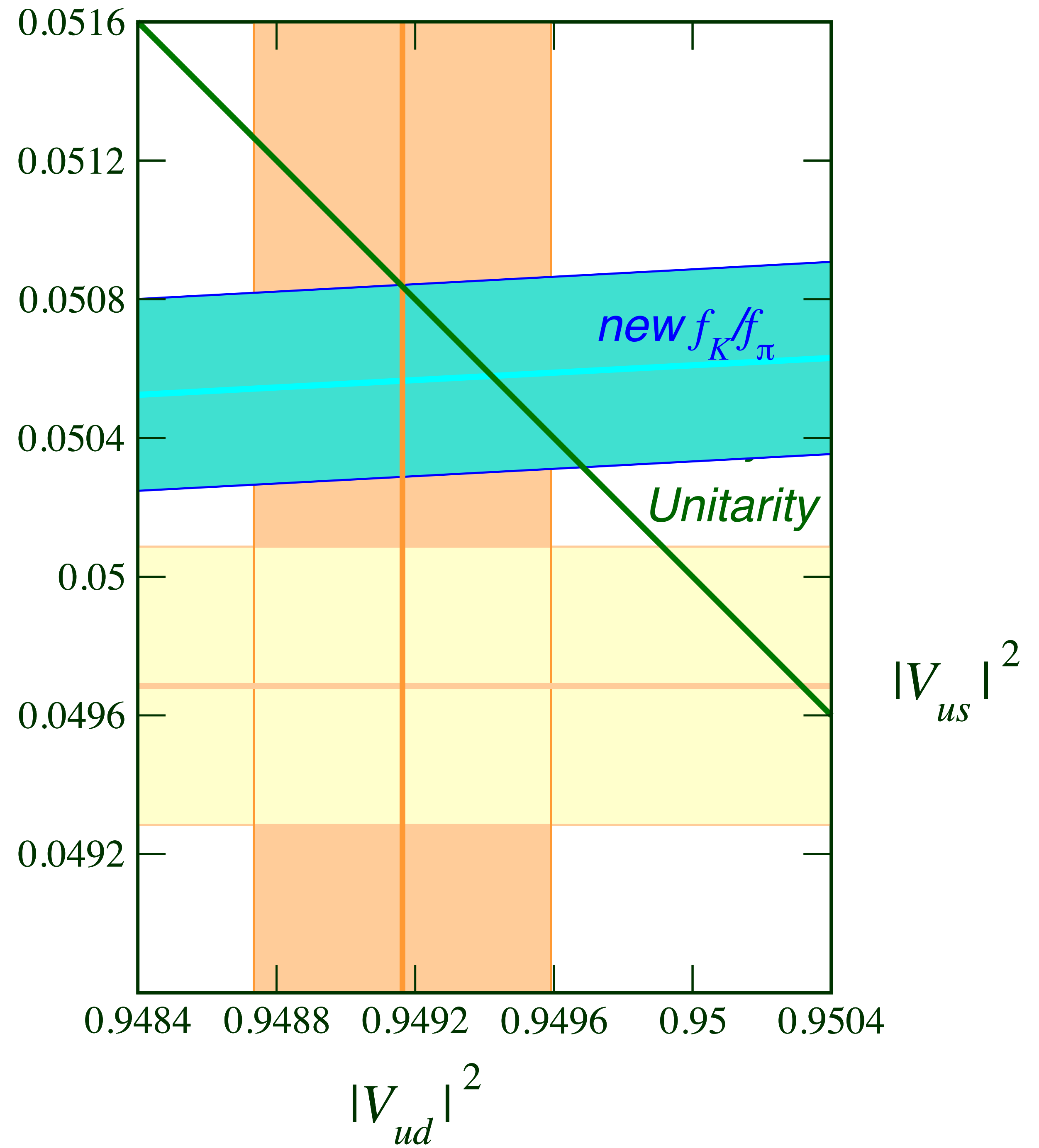
Semileptonic $K \to \pi l \nu$ for $|V_{us}|$

- aka the Cabibbo angle.
- Appears throughout flavor physics.
- esp. in first-row unitarity test: $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$?
- Now $|V_{us}|^2$ is as precise as $|V_{ud}|^2$ (from nuclear physics).
- Similar precision from f_K/f_π [arXiv:1407.3772].

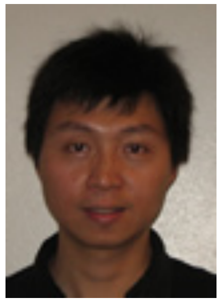


Semileptonic $K \to \pi l \nu$ for $|V_{us}|$

- aka the Cabibbo angle.
- Appears throughout flavor physics.
- esp. in first-row unitarity test: $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$?
- Now $|V_{us}|^2$ is as precise as $|V_{ud}|^2$ (from nuclear physics).
- Similar precision from f_K/f_π [arXiv:1407.3772].

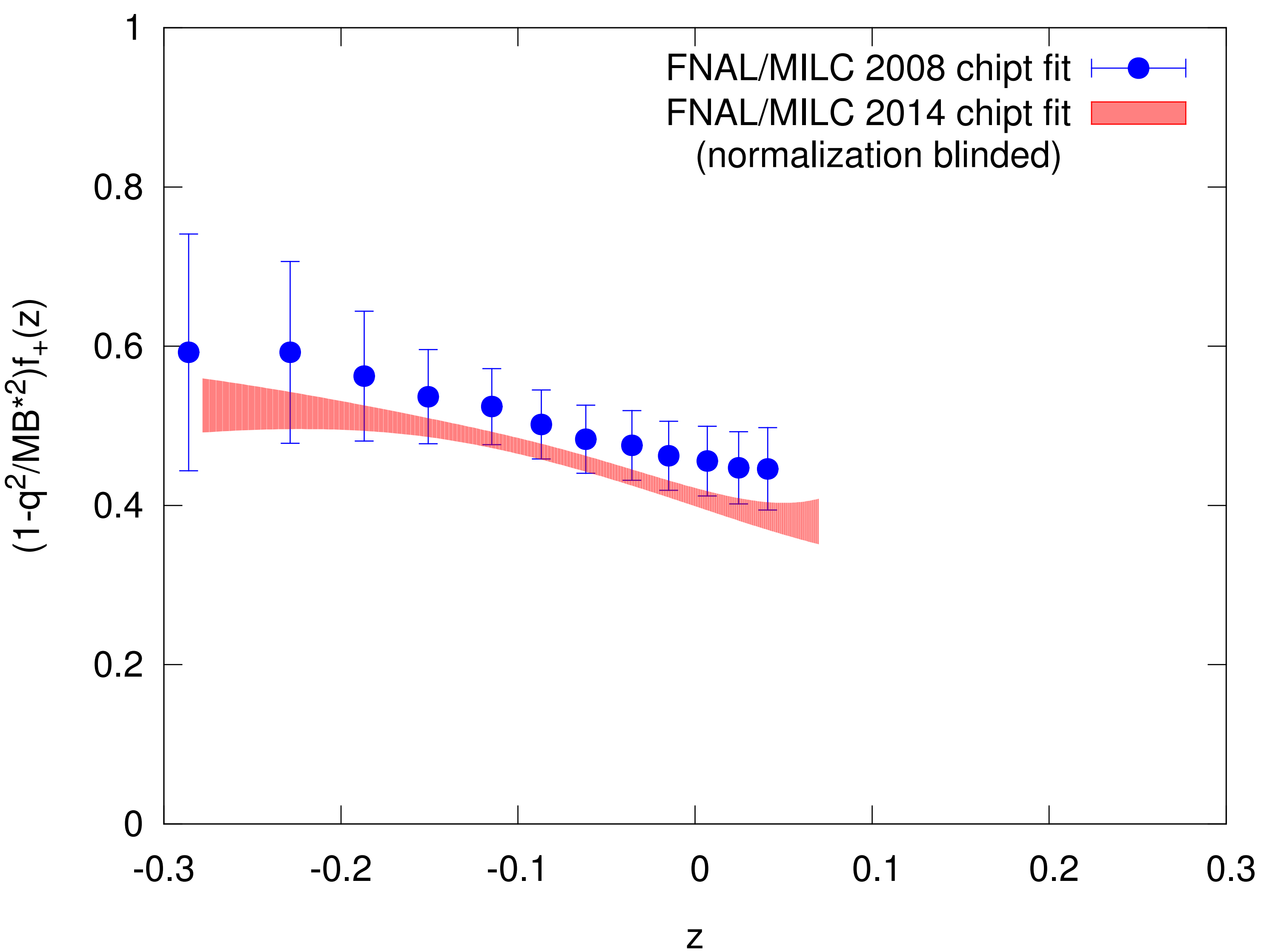


Semileptonic $B \to \pi l \nu$ for $|V_{ub}|$

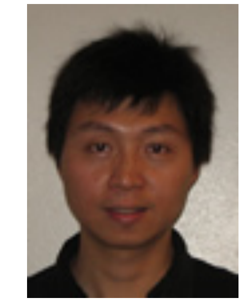


$$z = \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}}$$

- Much more precise than 2008.
- **PRELIMINARY! BLINDED!!**
- z variable extends range.
- Functional fitting method.
- Relative norm'n yields $|V_{ub}|$.
- Total error on $|V_{ub}|$: 4.1%.

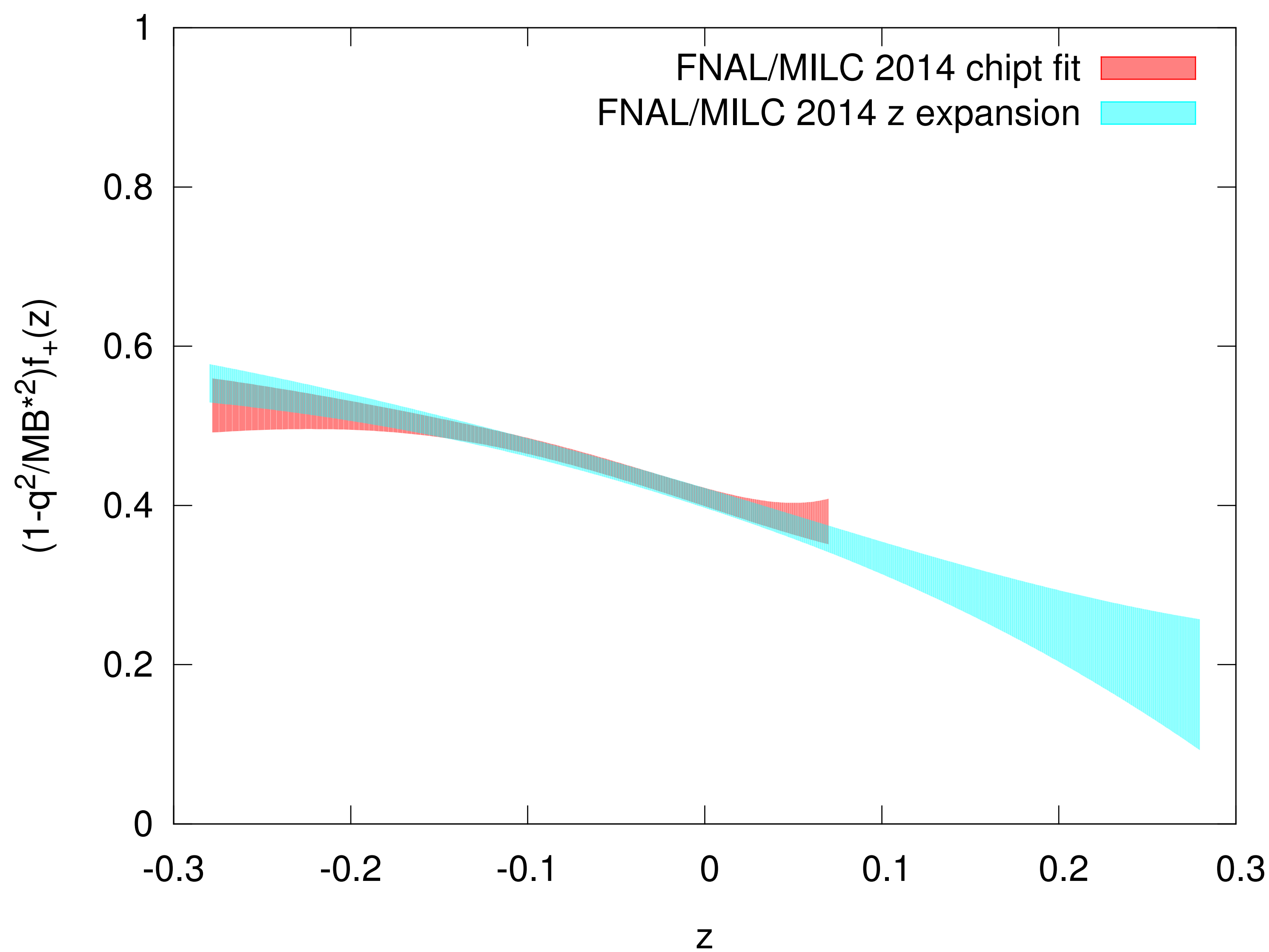


Semileptonic $B \to \pi l \nu$ for $|V_{ub}|$

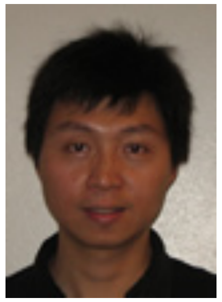


$$z = \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}}$$

- Much more precise than 2008.
- **PRELIMINARY! BLINDED!!**
- z variable extends range.
- Functional fitting method.
- Relative norm'n yields $|V_{ub}|$.
- Total error on $|V_{ub}|$: 4.1%.

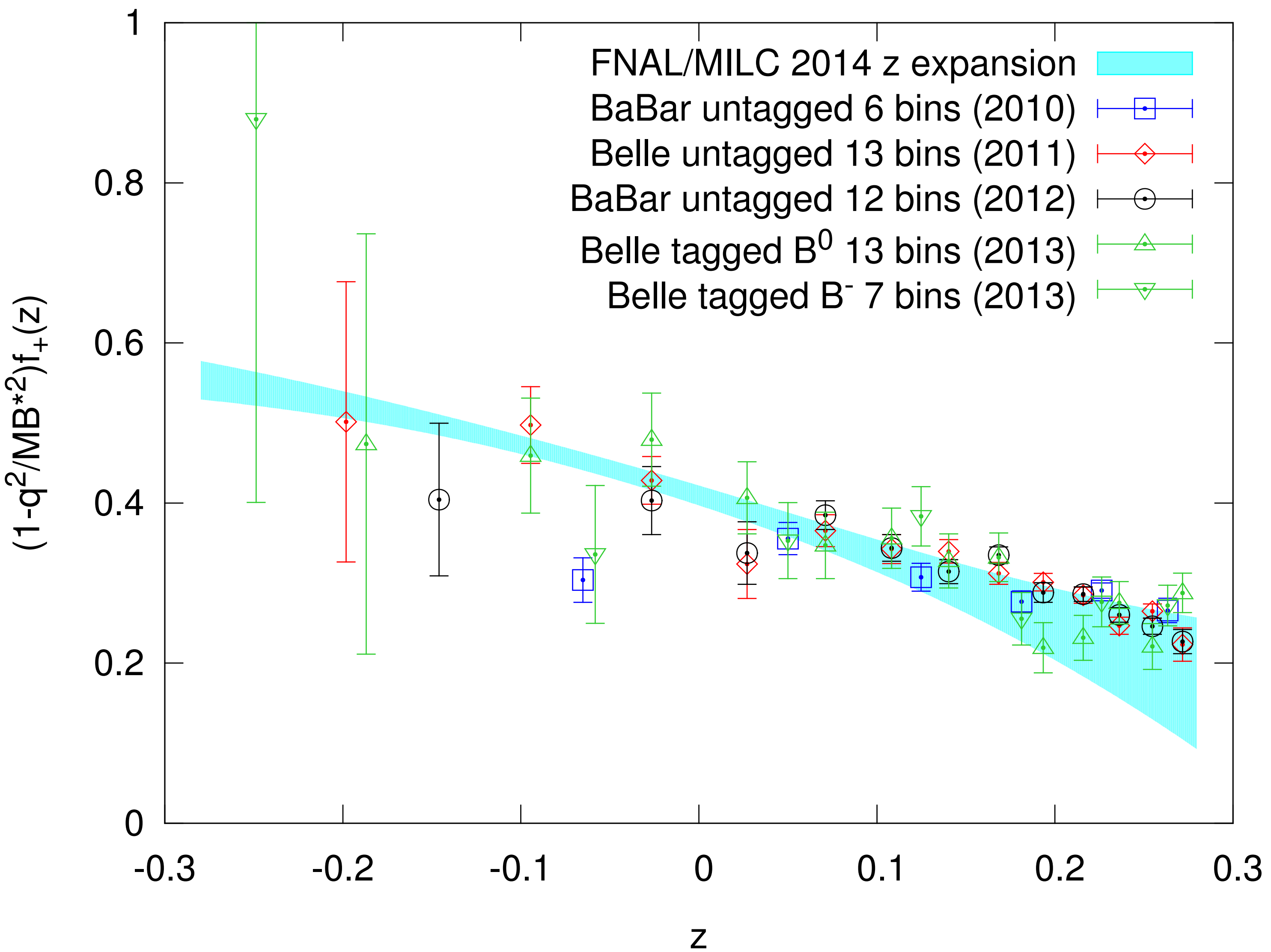


Semileptonic $B \to \pi l \nu$ for $|V_{ub}|$

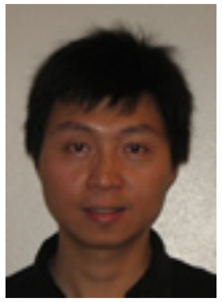


$$z = \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}}$$

- Much more precise than 2008.
- **PRELIMINARY! BLINDED!!**
- z variable extends range.
- Functional fitting method.
- Relative norm'n yields $|V_{ub}|$.
- Total error on $|V_{ub}|$: 4.1%.

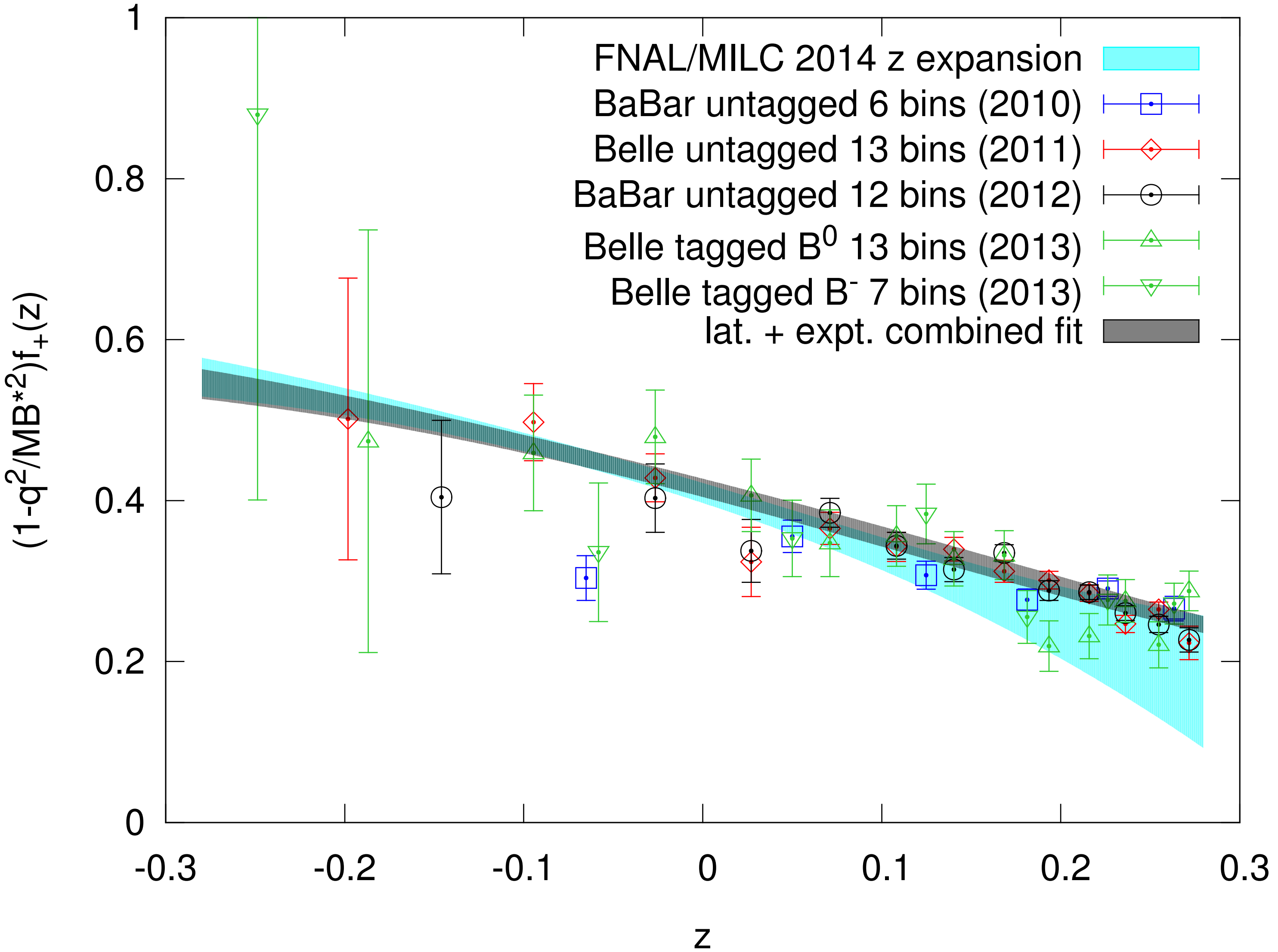


Semileptonic $B \to \pi l \nu$ for $|V_{ub}|$

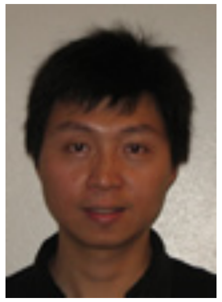


$$z = \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}}$$

- Much more precise than 2008.
- **PRELIMINARY! BLINDED!!**
- z variable extends range.
- Functional fitting method.
- Relative norm'n yields $|V_{ub}|$.
- Total error on $|V_{ub}|$: 4.1%.

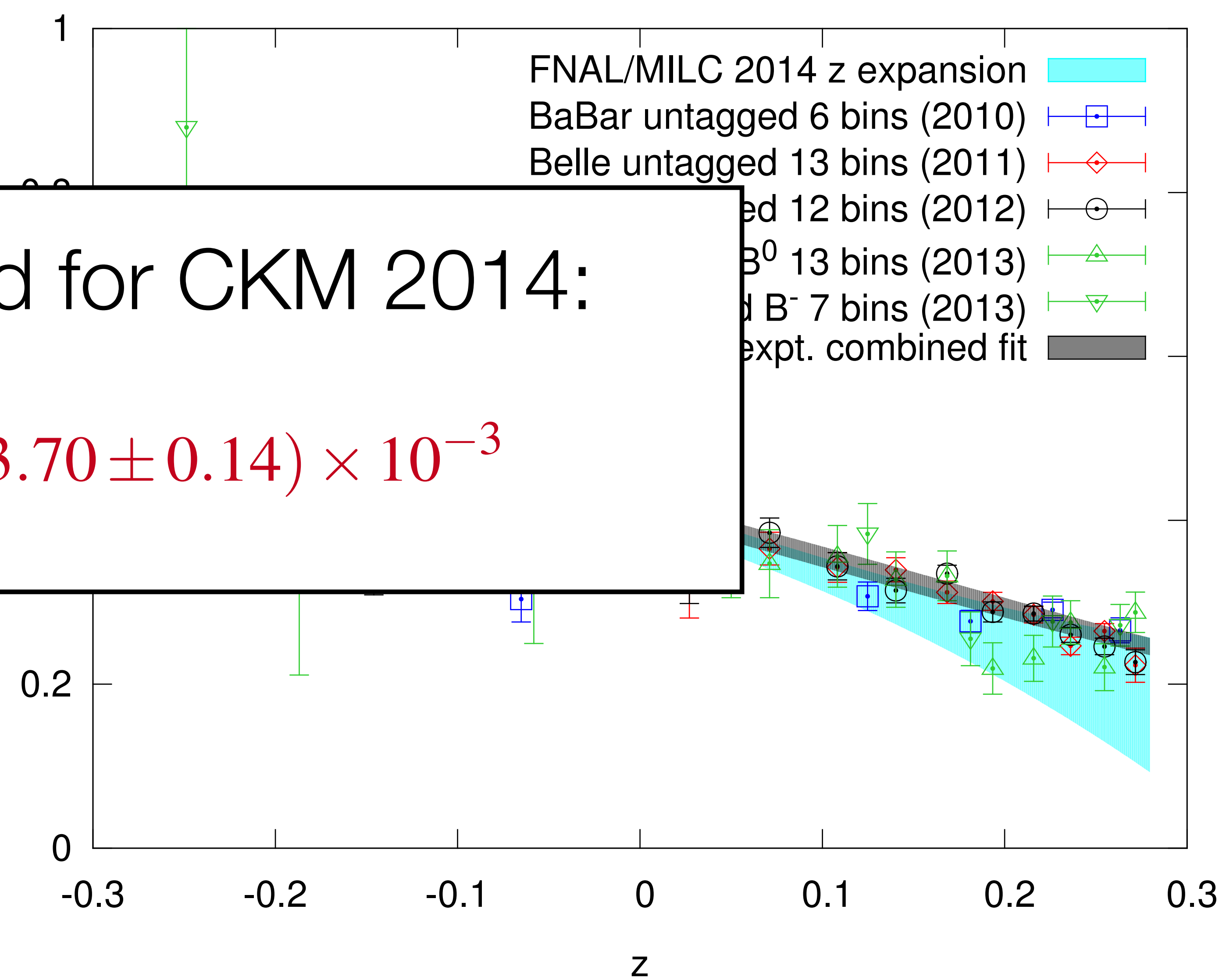


Semileptonic $B \to \pi l \nu$ for $|V_{ub}|$



$$z = \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}}$$

- Much more precise than 2008.
- **PRELIMINARY! BLINDED!!**
- z variable exten
- Functional fittin
- Relative norm'n yields $|V_{ub}|$.
- Total error on $|V_{ub}|$: 4.1%.



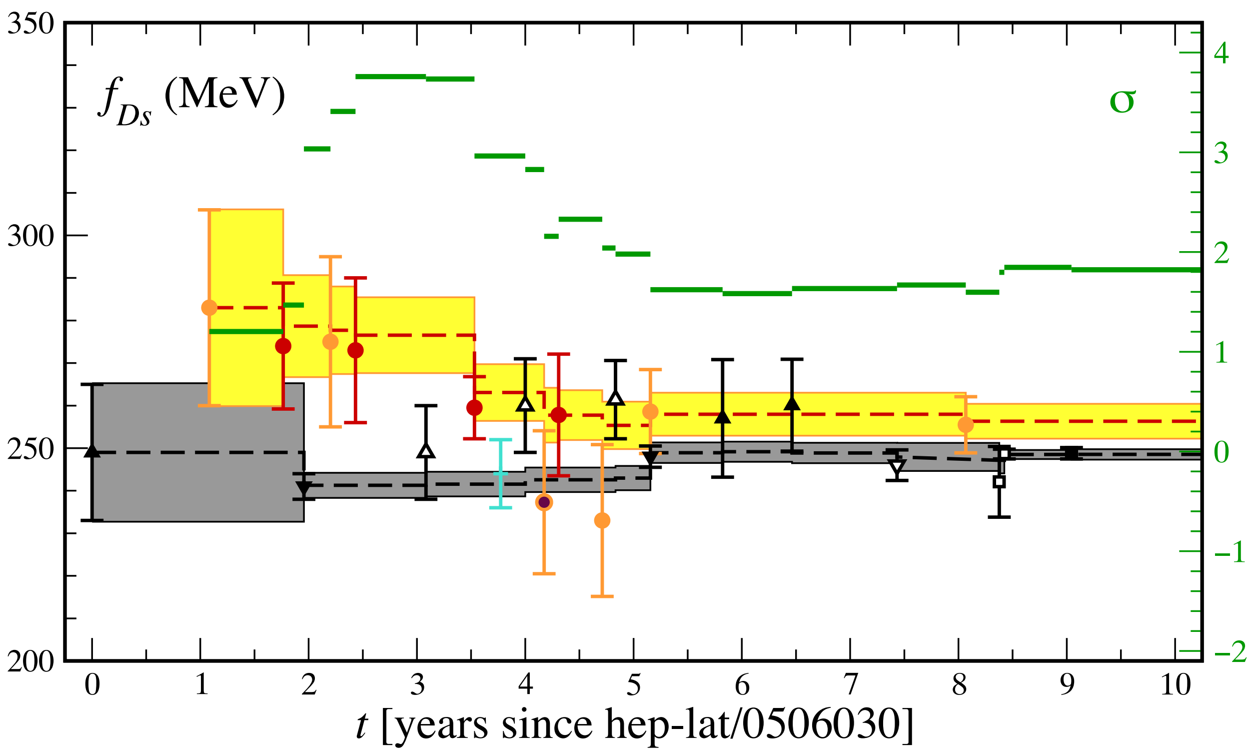
Unblinded for CKM 2014:

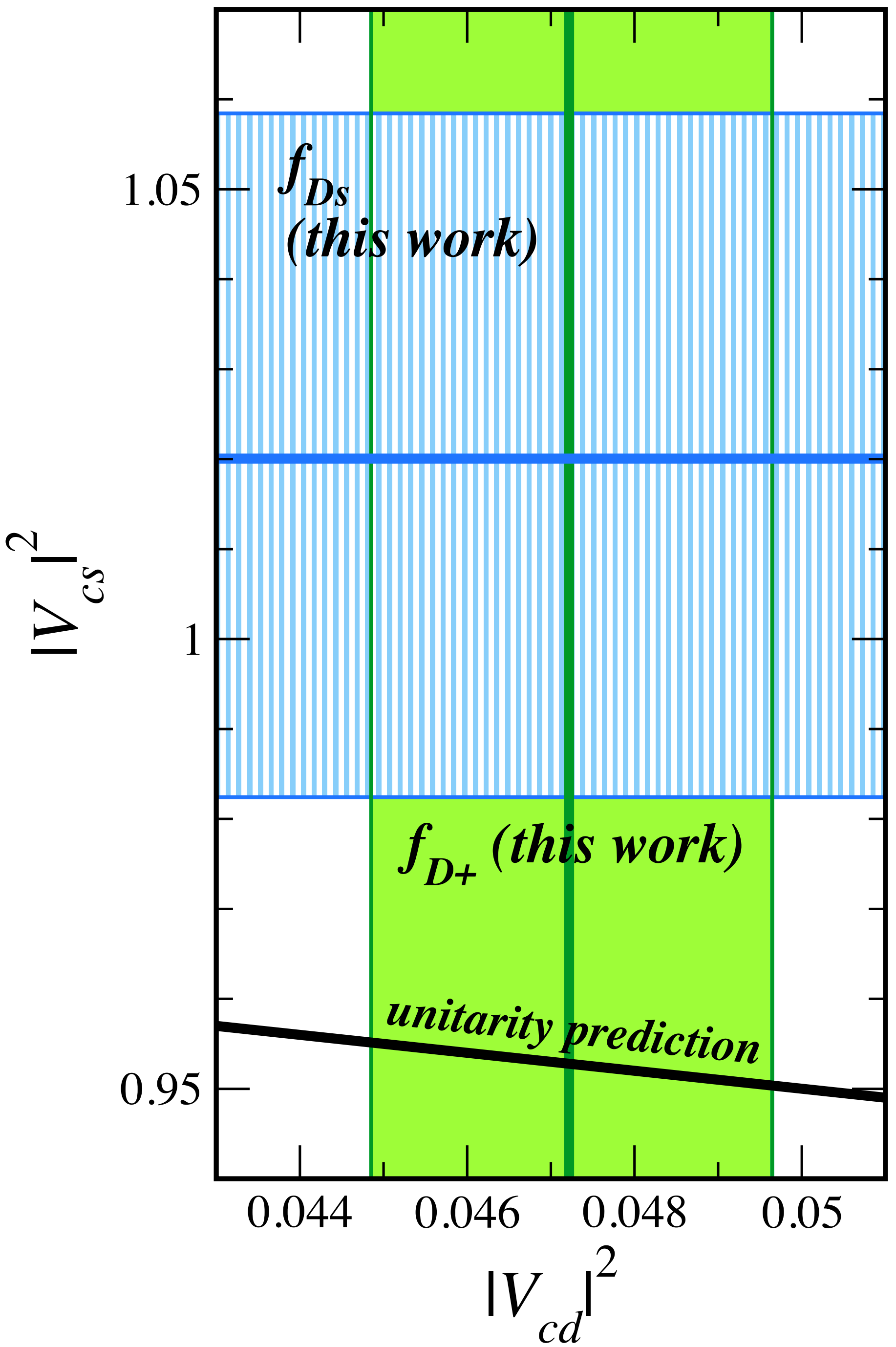
$$|V_{ub}| = (3.70 \pm 0.14) \times 10^{-3}$$

Leptonic $D \to l\nu$ and $D_s \to l\nu$ for $|V_{cd}|$ for $|V_{cs}|$

- HISQ action allows us to treat charmed quarks with the same method as strange, down, and up.

- Here the QCD uncertainty is smaller than the experimental uncertainty.

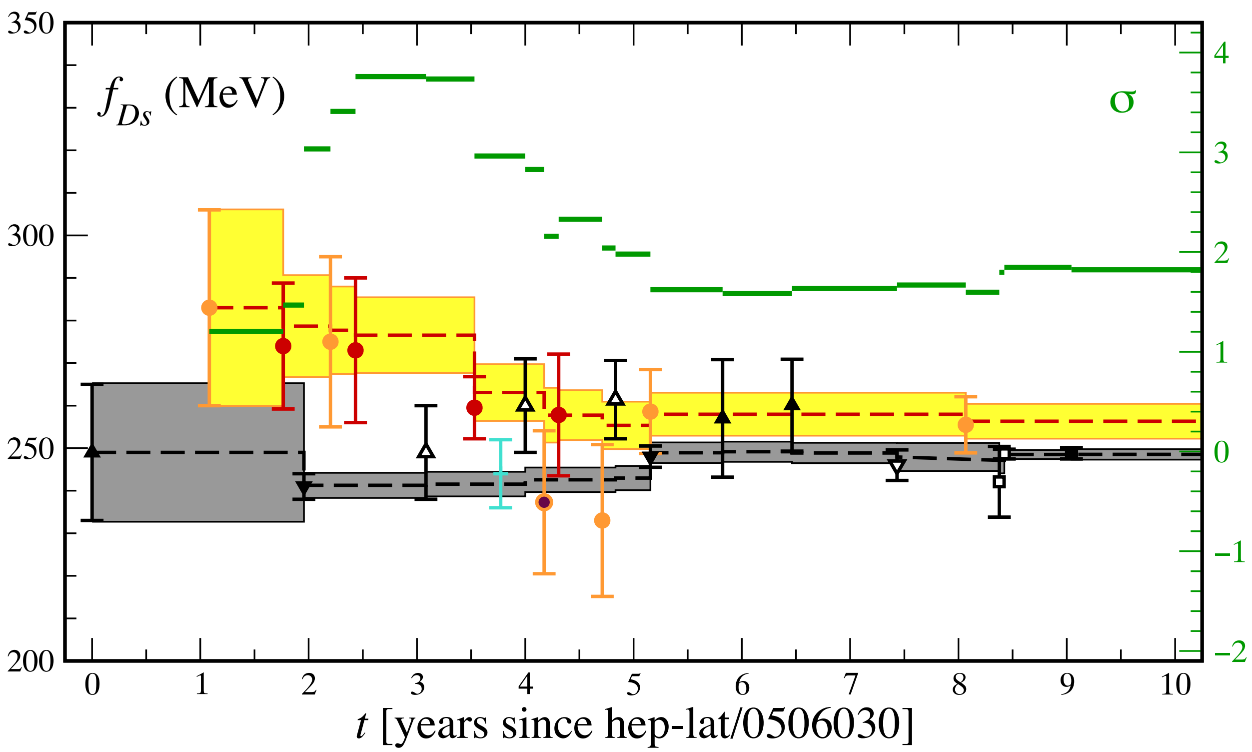


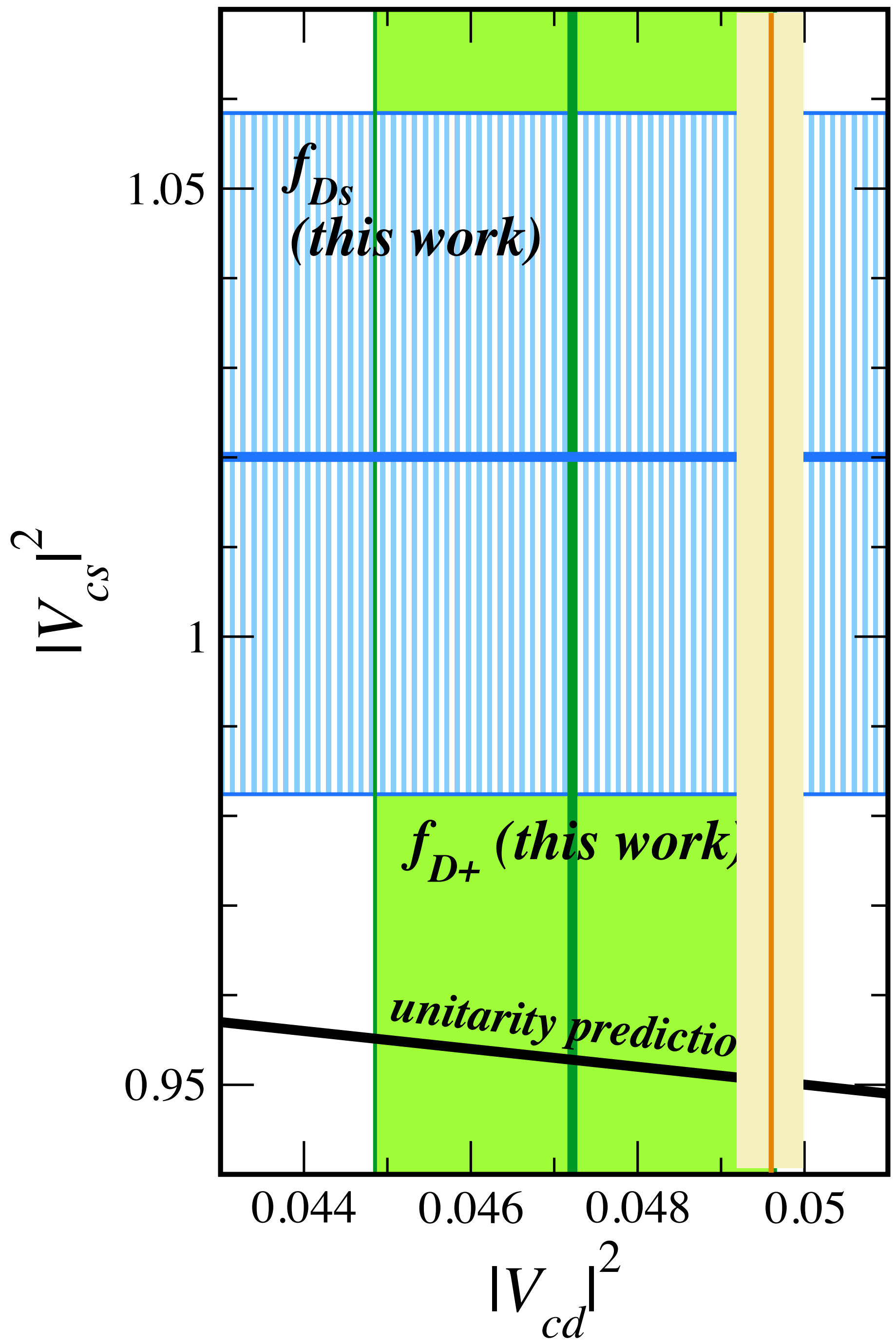


Leptonic $D \to l\nu$ and $D_s \to l\nu$ for $|V_{cd}|$ for $|V_{cs}|$

- HISQ action allows us to treat charmed quarks with the same method as strange, down, and up.

- Here the QCD uncertainty is smaller than the experimental uncertainty.





Lessons

- Lattice QCD plays a key role in $|V_{cb}|$, $|V_{ub}|$, $|V_{us}|$, and $|V_{cd}|$ & $|V_{cs}|$.
- Lattice QCD plays a crucial role for neutral-meson mixing (K, B, B_s).
- Suite of experiments and QCD theory (including lattice) show that CKM flavor violation and KM CP violation predominate.
- Still room (as well as need) for new physics: tension at 2–3σ level:
  - confidence level of global fit improves more, if NP in kaon mixing [LLV];
  - several distinct discrepancies at this level.

On the Light Cone, Without the Light Cone

Light-like Separation

- High-energy physics leads to particles that travel near the light cone.
  - parton densities (*pp* collisions) & distribution amplitudes (B decays).
- Euclidean field theory does not have a light cone.
- Can one find Euclidean (and perhaps finite-volume) observables that can be related, via effective field theory to similar information?
- For example, ideas by Ji to obtain the full x dependence of quark densities [*PRL* **110** (2013) 262002] has been put into practice [arXiv:1402.1462].
- Side-steps issues arising when discretizing high-dimension operators.

Intriguing Examples

- Can we extend these ideas and calculations to the gluon density?
    - The gluon density is poorly known and essential for LHC discoveries.
- Can we extend these ideas and calculations to the *B*-meson distribution amplitude?
    - The "inverse" moment is poorly known and essential for the description on nonleptonic *B* decays.

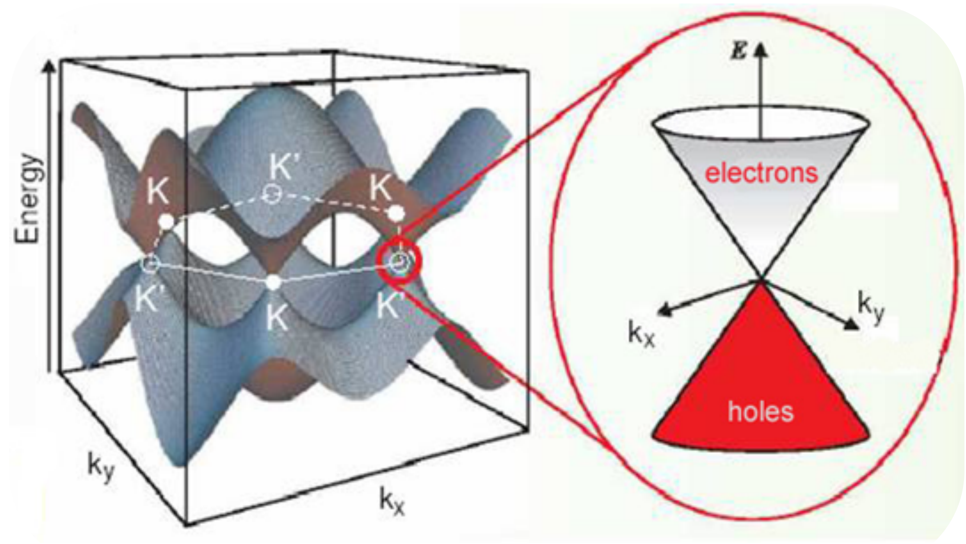
Beyond QCD

Dynamical Symmetry Breaking

- It is still possible that some kind of strong dynamics breaks $SU(2)\times U_Y(1)$.
- Needed ingredients:
    - large mass anomalous dimension ⇒ strong coupling;
    - very small β function ⇒ many length scales involved;
    - light scalar boson ⇐ Higgs-like candidate.
- Many length scales call out for effective field theories; strong coupling for lattice gauge theory.

Optical Lattices with Gauge Symmetries

- Relativistic (*i.e.*, $E = |\boldsymbol{k}|$) band structure in graphene:



- Possible to design optical lattices trapping cold atoms, such that symmetry is non-Abelian, as in lattice QCD [*e.g.*, arXiv:1211.2704].

- Use LGT to understand these systems & these systems to understand QCD.

- Activity in this field from Cirac [arXiv:1407.4995], Meurice [arXiv:1403.5238], and Wiese [arXiv:1409.7414].

Today’s Speakers, Session Chairs, and Pralines

IAS TUM Institute for Advanced Study

Kick-off Symposium of Hans Fischer Senior Fellow Dr. Andreas Kronfeld

Lattice Gauge Theory and Effective Field Theories

November 26, 2014 | 14:00 | TUM-IAS | Lichtenbergstr. 2 a, Garching

14:00 -14:15	**Gerhard Abstreiter**, TUM-IAS Welcome Remarks and Fellowship Nomination
14:15 -14:45	**Andreas Kronfeld**, Fermilab *"Lattice Gauge Theory and Effective Field Theory"*
14:45 -15:10	**Zoltan Fodor**, University of Wuppertal *"Lattice QCD: Hadron Spectrum and Thermodynamics"*
15:10 -15:35	**Simone Biondini**, TUM *"Effective Field Theories at Nonzero Temperature"*
15:35	Coffee Break
16:00 -16:25	**Stephan Paul**, TUM *"Challenging Low-Energy QCD: New Insight into the Light-meson Spectrum and Low-Energy Processes with Pions"*
16:25 -16:50	**Antonio Vairo**, TUM *"Determination of α_s from the QCD Static Energy"*
16:50 -17:15	**Gerhard Buchalla**, LMU *"Effective Field Theories Beyond QCD"*
17:15 - 17:40	**Siegfried Bethke**, Max Planck Institute for Physics *"LHC Physics"*
17:45-?	Reception
Co-organizer:	**Nora Brambilla**, TUM

Technische Universität München · Institute for Advanced Study
Lichtenbergstraße 2 a · 85748 Garching · Tel +49.89.289.10550 · info@tum-ias.de · www.tum-ias.de

European Commission